

# **Optimal Design of T<sup>2</sup> Multivariate Statistical Chart for Process Monitoring**

**M. A. Bin Shams**  
**Department of Chemical Engineering**  
**University of Bahrain, Isa Town**  
**Kingdom of Bahrain**

**O. Yuksel Orhan**  
**Chemical Engineering Department**  
**Hacettepe University**  
**Ankara, Turkey**

**E. Alper, K. Moorthy, J. Rafinejad, A. Saxena and A. Elkamel**  
**Chemical Engineering Department**  
**University of Waterloo**  
**Waterloo, ON N2L 3G1, Canada**

## **Abstract**

The objective of this paper is to design the T<sup>2</sup> statistical control chart based on the economical criterion to monitor product quality of the Tennessee Eastman process. An optimization algorithm is proposed to minimize monitoring costs. A sensitivity analysis is conducted on the cost parameters of the economical algorithm to determine their effect on the cost function. The implementation of a multivariate economical criterion on the design of T<sup>2</sup> control chart provides an improved basis for the evaluation and repair of out of control states and result in monitoring cost minimization via optimal sampling schedules. These benefits are in addition to those that exist in the utilization of a statistical model that are currently utilized. To develop the economic design of the T<sup>2</sup> monitoring chart, an expected cost function pioneered by Douglas Montgomery was used in this investigation to estimate monitoring costs and optimize the upper control limit. Next the chart was modified for the Tennessee Eastman Plant and a preliminary estimate of \$290 of savings per cycle was realized. Sensitivity analysis was performed on the expected cost function parameters and decision variables. Sampling costs were determined to correlate positively with cost savings per cycle, while penalty costs associated with out-of-control operation correlated negatively with savings. Analysis on the decision variable n (the number of samples per cycle), indicates that the expected cost function optimization resulted in the same convergence point; a global minimum may have been achieved.

## **Keywords**

X-bar control charts, Multivariate model, T<sup>2</sup> Control Charts

## **Biography**

**M.A. Binshams** holds a Bachelor degree and a Master degree in Process Engineering from the University of Bahrain and the University of Manchester, respectively. He got his Ph.D. degree in Chemical Engineering from the University of Waterloo. At Waterloo, he conducted research on Process Control and Fault detection and diagnosis. He is currently an Assistant Professor in the Department of Chemical Engineering at the University of Bahrain. He has also experience as a process engineer at Yokogawa (a leading manufacturer and supplier of industrial automation & process control, test & measurement, information systems and industrial services). His research interests are in process control, systems engineering, and fault detection and diagnosis with applications to the oil and gas industry.

**E. Alper** is a professor of chemical engineering at Hacettepe University. He served as chairman of the department from 2004 - 2007. He holds a PhD in Chemical from Cambridge University. He is internationally recognized for his research on modeling and analysis of complex systems, mass transfer with chemical reaction in multiphase systems (including catalytic multiphase reactors), and the kinetics and selectivity of absorption of hydrogen sulphide and carbon dioxide and carbonyl sulphide into alkanolamine solutions. He published over 150 articles and conference proceedings in these areas. He served as the editor of the Turkish Chemical Engineering Journal, a member of the editorial board of the Journal of Gas Separation and Purification, and is currently serving as a member of the Commission of Special Experts for the Chemical Industry, 9<sup>th</sup> Plan, State Planning Organisation.

**A. Elkamel** is a professor of Chemical Engineering at the University of Waterloo, Canada. He holds a B.S. in Chemical and Petroleum Refining Engineering and a B.S. in Mathematics from Colorado School of Mines, an M.S. in Chemical Engineering from the University of Colorado-Boulder, and a Ph.D. in Chemical Engineering from Purdue University. His specific research interests are in computer-aided modeling, optimization, and simulation with applications to the petroleum and petrochemical industry. He has contributed more than 250 publications in refereed journals and international conference proceedings and serves on the editorial board of several journals, including the International Journal of Process Systems Engineering, Engineering Optimization, International Journal of Oil, Gas, Coal Technology, and the Open Fuels & Energy Science Journal.

**K. Moorthy, J. Rafinejad, A. Saxena** are fourth year students at the University of Waterloo.