

# **Optimizing Cleaning Schedules of Heat Exchanger Networks**

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## **Abstract**

Fouling in Heat Exchangers is a serious operating problem in many industries. It drastically reduces heat transfer effectiveness and consequently, the rate of heat transfer. Fouling also causes difficulty in maintaining key temperatures within their operating envelopes, as well as it imposes severe hydraulic limitations to passing fluids through the heat exchanger. To combat fouling, heat exchangers must be periodically removed from service and cleaned. This is a costly expense, but not taking the heat exchanger out of service proves costly to downstream operations. More often than not, the undesired outlet temperature from the heat exchanger would demand a higher energy consumption further downstream to mitigate the problem. This trade-off implies an optimal time to clean the heat exchanger. In this study an approach was developed where operating process data can be used to predict the rate of fouling and be used in an optimization model to generate the optimal cleaning schedule. The project served to illustrate this idea by employing it in a rapidly fouling Heat Exchanger Network (HEN). A HEN in a SAGD Facility is considered and potential savings of \$30,000 per month are illustrated through the use of this approach. Management of fouling is a multi-billion dollar global problem and our solution has been proven to eliminate substantial amounts of unnecessary cleaning expenditures.

## **Keywords**

Optimization, MINLP, Heat exchanger networks, Scheduling

## **1. Introduction and background**

Heat Exchanger fouling is one of the most common and troublesome issues in process industries. Fouling can lead to losses in operational efficiency and ultimately increase a heat exchanger's maintenance/operational cost. The total fouling related costs for major industrialised nations is estimated to exceed US\$4.4 Billion annually (Ibrahim, 2012), or roughly 1% of their GDP. Evidently, fouling related costs are a major pain point for companies in a various range of industries. An exchanger will typically foul up as foulants in process streams begin in to agglomerate on the surface of tubes. There are two ways of understanding this phenomena: 1) a build-up of foulants adds an extra layer of thermal resistance; thereby reducing the Overall Heat Transfer Coefficient (OHTC). This reduces total heat transfer effectiveness between process streams, and 2) a build-up of foulants also increases the frictional pressure drop across the heat-exchanger, thereby limiting the amount of flow that can be passed through the exchanger.

To counter-act fouling, heat exchangers are commonly taken out of service for cleaning. The typical modes of cleaning are as follows: 1) chemical Cleaning – Exchangers are taken out of service and a chemical solution is injected to extract out the foulant materials. The cost of these is anywhere from \$ 10'000 - \$ 50'000 (Ibrahim, 2012). A major contributor to high Operating Expenditures at any plant. This takes about a day and typically engineering service companies provide this service. Some companies (for e.g. MEG Energy in their Oil Sands facility) tend to perform bake-outs. This involves shutting down the supply of the cold stream and heating up the exchanger with the hot stream. The increase in temperature tends to eliminate deposited foulants. This ensures that the Heat Exchanger never goes out of service, and 2) mechanical Cleaning – these methods include the injection of molded plastic cleaners (PIGS) that go inside the tube and remove fouling through mechanical means. These methods are commonly employed where Chemical Cleaning methods do not adequately eliminate fouling.

Consequently, Heat Exchanger Cleanings amount to a massive operating expenditure for many operating plants. It is important for plant engineers to understand the trade-off that exists while scheduling heat exchanger cleanings. In the case of a single heat exchanger, cleaning too frequently will substantially increase the cleaning expenditures. However, cleaning too infrequently has the potential to increase energy consumption in upstream/downstream operations due to limited heat transfer capabilities of the fouled heat exchanger. In both cases, operating cost will go up. The trade-off is apparent, and displayed below in Figure 1.

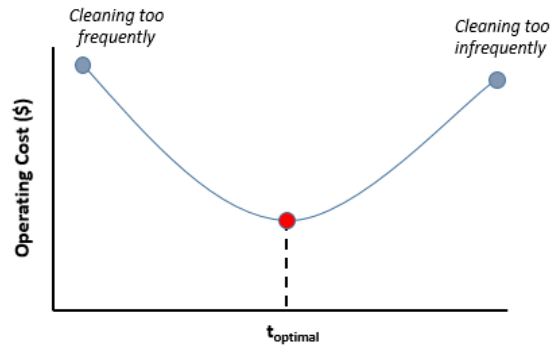


Figure 1. Operating Cost (\$) vs. Run Time Trade-Off for a single heat exchanger

Figure 2 analyzes the OHTC of an individual heat exchanger as a function of time. The red curve illustrates the depreciation of this important parameter and the red area is a multiple of the total heat transferred. The green area represents a multiple of total heat lost due to fouling (and consequential cleaning). It is apparent from this figure that an optimal run time can be calculated for this single heat exchanger that minimizes the total heat lost (or maximizes total heat transferred) in a definite period of time.

The ideas developed above for a single heat exchanger can be extended to a Heat Exchanger Network (HEN). Scheduling heat exchanger cleanings for HENs is much more complicated and requires a much more holistic approach than that for a single heat exchanger. However, the idea remains the same. The intent is to minimize operating cost all while meeting a set of pre-defined process constraints. The basic premise of this study is to solve the scheduling problem that commonly affects many process industries. The current scheduling methods comprise of rudimentary discussions between engineers and do not take a holistic engineering approach. Thus, the objective can be formally described as: Develop a software that is capable of tracking the fouling behavior of a specific heat exchanger network using process data; and further generate optimal cleaning schedules using mathematical optimization techniques.

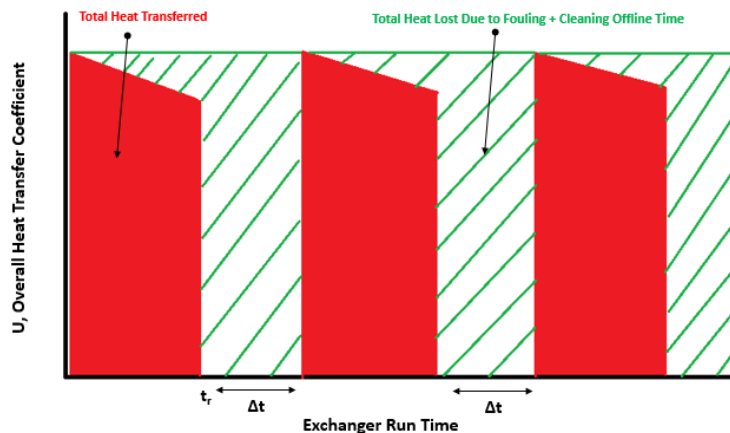


Figure 2. Analysis of an OHTC curve for a single heat exchanger

The market for reducing fouling related expenditures is huge. We are not directly competing with anti-fouling chemicals divisions of many companies, but instead focused on using data analytics to improve decision making. As such, there are two competitors in this relatively un-tapped market: 1) Shell HEAT4N Software: This monitoring software has been developed by Shell Global Solutions. It contains a very rudimentary approach to fouling calculations and contains a first degree optimization model which is only really applicable to a single heat exchanger, and not a network as a whole. Other drawbacks of the software are poor Graphical User Interface (GUI), and the reference

overall heat transfer coefficient (U) is fixed based on design conditions. This can cause erroneous values should the inlet conditions drastically change during the operation of the heat exchanger. 2) Emerson Process Monitoring Software: This software from Emerson connects to the DCS and provides temperature and pressure measurements that are trended and analyzed to alert operators of potential fouling considerations. The major drawback to this is that it does not actually provide an opportunity to optimize scheduling of heat exchanger cleaning.

## 2. Design methodology

After many iterations of generating an industrially acceptable software for the problem, the team agreed on the following architecture. The main elements of this architecture reside in the red boxes (software back-end). The discussion will remain focused on these elements. While a lot of work was conducted on the front-end part of the software (green boxes), a thorough discussion of these will remain out of scope for this report.

### 2.1 Data Manipulation and Filtration

In this portion of the software, data is collected from the plant historian and filtered to eradicate any erratic process data (up to a year's worth of data is considered). The primary data collected will usually be flow rate, temperature and pressures at the inlet and outlet of each heat exchanger. The filtration methods being used in the preliminary version of the software are moving average filters.

### 2.2 Fouling/OHTC Calculations and Statistical Regression

Modified data is then used to calculate OHTC and Fouling Factor. The mathematical essence of these calculations is described in later sections. The calculated OHTC is then regressed as a function of run time for past runs for each heat exchanger. The statistical regression parameters are an important input to the optimization model. Hence, the statistical methods used must be very accurate.

### 2.3 Optimization Model Generation and Solution

This section of the software solves a pre-defined optimization model. The constraints of this model are subject to the heat exchanger network at hand. However, some constraints depend on the statistical regression results for each heat exchanger in the network. The objective function serves to minimize the operating cost. The output of this model is the optimal cleaning schedule. More discussion on all components of the software will be presented in the context of a case study below.

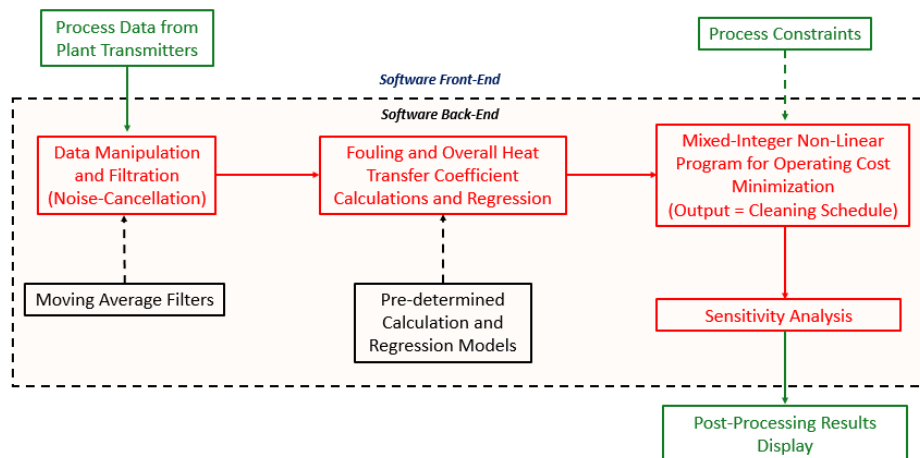


Figure 3. Software Architecture of the Proposed Solution

## 3. Model

### 3.1 Fouling & Overall Heat Transfer Coefficient Calculations

This section covers preliminary heat transfer theory utilized while calculating the Overall Heat Transfer Coefficient (OHTC) from process data. A simple enthalpy balance on the two fluids yields:

$$\begin{aligned}\dot{Q} &= M_h \cdot C_{p_h} \cdot (T_{h,in} - T_{h,out}(t)) \\ \dot{Q} &= M_c \cdot C_{p_c} \cdot (T_{c,out}(t) - T_{c,in})\end{aligned}$$

From heat transfer theory, the rate of heat transfer in the arbitrary heat exchanger above can be modelled as:

$$\dot{Q} = U(t) \cdot A \cdot \Delta T_{LM} \cdot F$$

Solving for U (OHTC) yields:

$$U(t) = \frac{\dot{Q}}{A \cdot \Delta T_{LM} \cdot F} = \frac{M_h \cdot C_{p_h} \cdot (T_{h,in} - T_{h,out}(t))}{A \cdot \Delta T_{LM} \cdot F} = \frac{M_c \cdot C_{p_c} \cdot (T_{c,out}(t) - T_{c,in})}{A \cdot \Delta T_{LM} \cdot F}$$

The fouling factor at each time is easily computed through:

$$f = \frac{1}{U(t)} - \frac{1}{U_{clean}}$$

However, it must be noted that  $U_{clean}$  is a function of the operating conditions (or inlet process conditions). In our case, we will assume these to be fixed. Notice also that fouling factor is simply a modified representation of the OHTC. It is merely used in our calculations, but it is useful to generate for monitoring purposes. We will only consider U or OHTC for further calculations. Now that U can be calculated at various times during a run, statistical analysis can be used to fit an empirical model. From a close analysis of the data, an exponential functions serves best to describe the decaying U function. This can be expressed as:

$$U(t) = U_o e^{-kt}$$

where  $U_o$  and  $k$  are the regression parameters. Moving average filters are used to better filter the data at hand. This is mathematically represented as:

$$y_s(i) = \frac{1}{2N+1} (y(i+N) + y(i+N-1) + \dots + y(i-N))$$

where,  $y_s(i)$  is the smoothed value for the  $i^{th}$  data point,  $N$  is the number of neighbouring data points on either side of  $y_s(i)$ .

### 3.2 Optimization model

The mixed integer non-linear programming (MINLP) optimization model intakes the results of the fouling analysis and generates optimal cleaning decisions for each heat exchanger in the network, for a pre-defined time horizon. The key decision variables are the cleaning of a specific heat exchanger in a specific period. Mathematically speaking, this translates to:

$$y_{n,p} = \begin{cases} 1 & \text{(if heat exchanger n is in service during period p)} \\ 0 & \text{(if heat exchanger n is out of service during period p)} \end{cases}$$

where  $n$  represents the number of heat exchangers in the network and  $p$  represents the number of periods. The time horizon has been discretized into  $p$  periods, hence converting this continuous optimization problem into a discrete one. This reduces the computational complexity and effort, and also accounts for logistical constraints. Additionally, other decisions variables include:  $T_{n,p}^{h,out}$  outlet temperature of the hot stream in heat exchanger  $n$ , with a given period  $p$ ,  $T_{n,p}^{c,out}$  outlet temperature of the cold stream in heat exchange  $n$ , within a given period  $p$ , and  $U_{n,p}$  overall heat transfer coefficient in heat exchanger  $n$ , within a given period  $p$ .

The simulation of the heat exchanger network is a critical component of the optimization model. As will be described below, the statistical analysis of fouling data is a direct input to this component of the model. Consider a single heat exchanger with a fixed heat transfer area  $A$ , hot inlet stream temperature and mass flow rate of  $T_{h,in}$ ,  $M_h$  respectively and cold inlet stream temperature and mass flow rate of  $T_{c,in}$ ,  $M_c$ . If the performance of the heat exchanger is known through its overall heat transfer coefficient's behavior as a function of time, then it is possible to solve for the outlet temperature of both the streams. This is mathematically illustrated as follows, let  $\dot{Q}$  denote total rate of heat transfer between the hot and the cold streams. A simple thermodynamic heat balance between the two streams yield the following equations:

$$\begin{aligned}\dot{Q} &= M_h \cdot C_{p_h} \cdot (T_{h,in} - T_{h,out}) \\ \dot{Q} &= M_c \cdot C_{p_c} \cdot (T_{c,out} - T_{c,in})\end{aligned}$$

From heat transfer theory, the rate of heat transfer in the arbitrary heat exchanger above can be modelled as:

$$\dot{Q} = U(t) \cdot A \cdot \Delta T_{LM} \cdot F$$

The Log-Mean Temperature used in the equation above is given by:

$$\Delta T_{LM} = \frac{(T_{h,out} - T_{c,in}) - (T_{h,in} - T_{c,out})}{\ln \frac{(T_{h,out} - T_{c,in})}{(T_{h,in} - T_{c,out})}}$$

The correction factor, F, can be evaluated using complex models present in literature. However, for the purposes of this study, it is anticipated that the variation in F is minimal at best. Hence, the constant design value of F will be used for each heat exchanger in this simulation. The above equations can be simultaneously solved to yield expressions for  $T_{h,out}$  and  $T_{c,out}$ . The results are shown below:

$$T_{h,out} = \left[ \frac{\exp\left(-\frac{U(t) \cdot A}{M_h C_{p_h}} F \left(\frac{M_h C_{p_h}}{M_c C_{p_c}} - 1\right) - 1\right)}{\exp\left(-\frac{U(t) \cdot A}{M_h C_{p_h}} F \left(\frac{M_h C_{p_h}}{M_c C_{p_c}} - 1\right) - \frac{M_h C_{p_h}}{M_c C_{p_c}}\right)} \right] T_{c,in} - \left[ \frac{\frac{M_h C_{p_h}}{M_c C_{p_c}} - 1}{\exp\left(-\frac{U(t) \cdot A}{M_h C_{p_h}} F \left(\frac{M_h C_{p_h}}{M_c C_{p_c}} - 1\right) - \frac{M_h C_{p_h}}{M_c C_{p_c}}\right)} \right] T_{h,in}$$

$$T_{c,out} = \left[ \frac{\left(1 - \frac{M_h C_{p_h}}{M_c C_{p_c}}\right) \exp\left(-\frac{U(t) \cdot A}{M_h C_{p_h}} F \left(\frac{M_h C_{p_h}}{M_c C_{p_c}} - 1\right)\right)}{\exp\left(-\frac{U(t) \cdot A}{M_h C_{p_h}} F \left(\frac{M_h C_{p_h}}{M_c C_{p_c}} - 1\right) - \frac{M_h C_{p_h}}{M_c C_{p_c}}\right)} \right] T_{c,in} + \left[ \frac{\frac{M_h C_{p_h}}{M_c C_{p_c}} \cdot \exp\left(-\frac{U(t) \cdot A}{M_h C_{p_h}} F \left(\frac{M_h C_{p_h}}{M_c C_{p_c}} - 1\right)\right)}{\exp\left(-\frac{U(t) \cdot A}{M_h C_{p_h}} F \left(\frac{M_h C_{p_h}}{M_c C_{p_c}} - 1\right) - \frac{M_h C_{p_h}}{M_c C_{p_c}}\right)} \right] T_{h,in}$$

In order to visually simplify the expressions above, the following intermediate variables are defined and utilized for the remainder of this report:

$$k_1 = \frac{M_h C_{p_h}}{M_c C_{p_c}}$$

$$k_2(t) = \frac{U(t) \cdot A}{M_h C_{p_h}}$$

$$M_h = \frac{\left[ \frac{M_h C_{p_h}}{M_c C_{p_c}} \cdot \exp\left(-\frac{U(t) \cdot A}{M_h C_{p_h}} F \left(\frac{M_h C_{p_h}}{M_c C_{p_c}} - 1\right)\right) \right]}{\exp\left(-\frac{U(t) \cdot A}{M_h C_{p_h}} F \left(\frac{M_h C_{p_h}}{M_c C_{p_c}} - 1\right) - \frac{M_h C_{p_h}}{M_c C_{p_c}}\right)} = \frac{k_1 (\exp(-k_2 F (k_1 - 1)) - 1)}{\exp(-k_2 F (k_1 - 1)) - k_1}$$

$$M_c = \frac{\left[ \left(1 - \frac{M_h C_{p_h}}{M_c C_{p_c}}\right) \exp\left(-\frac{U(t) \cdot A}{M_h C_{p_h}} F \left(\frac{M_h C_{p_h}}{M_c C_{p_c}} - 1\right)\right) \right]}{\exp\left(-\frac{U(t) \cdot A}{M_h C_{p_h}} F \left(\frac{M_h C_{p_h}}{M_c C_{p_c}} - 1\right) - \frac{M_h C_{p_h}}{M_c C_{p_c}}\right)} = \frac{(1 - k_1) \cdot (\exp(-k_2 F (k_1 - 1)) - 1)}{\exp(-k_2 F (k_1 - 1)) - k_1}$$

Substituting the equations above reduce the outlet temperature equations to the following form:

$$T_{c,out} = M_h T_{h,in} + M_c T_{c,in}$$

$$T_{h,out} = T_{h,in} - \left(\frac{1}{k_1}\right) (T_{c,out} - T_{c,in})$$

The overall heat transfer coefficient behavior as a function of time is deciphered from the non-linear regression analysis conducted previously and is of the form:

$$U(t) = U_o \cdot \exp(-k \cdot t)$$

The equations above can help simulate the outlet temperature and heat transfer rate of the arbitrary exchanger described above. The binary nature of the decision variables makes it very convenient to discretize the continuous simulation equations. The discretized outlet temperature and overall heat transfer equations are presented below:

$$T_{n,p}^{c,out} = M_h y_{n,p} \cdot T_{n,p}^{h,in} + (1 - y_{n,p} + y_{n,p} M_c) \cdot T_{n,p}^{c,in}$$

$$T_{n,p}^{h,out} = T_{n,p}^{h,in} - \frac{1}{k_1} (T_{n,p}^{c,out} - T_{n,p}^{c,in})$$

$$U_{n,p} = U_{n,p-1} \cdot \exp(-k_n \Delta t_p) \cdot y_{n,p} + (1 - y_{n,p}) \cdot U_{o_n}$$

where  $U_{o_n}$  and  $k_n$  are regression parameters for the nth heat exchanger. Additionally, since the hot outlet streams of exchangers 1, 2, 3 & 4 serve as the inlet to exchangers 5 & 6, the corresponding inlet temperature to heat exchanger 5 & 6 is represented by:

$$T_{5,p}^{h,in} = \frac{(y_{1,p} \cdot T_{1,p}^{h,out} + y_{2,p} \cdot T_{2,p}^{h,out} + y_{3,p} \cdot T_{3,p}^{h,out} + y_{4,p} \cdot T_{4,p}^{h,out})}{3}$$

$$T_{6,p}^{h,in} = \frac{(y_{1,p} \cdot T_{1,p}^{h,out} + y_{2,p} \cdot T_{2,p}^{h,out} + y_{3,p} \cdot T_{3,p}^{h,out} + y_{4,p} \cdot T_{4,p}^{h,out})}{3}$$

The above equation assumes a constant mass flow rate distribution between Exchangers 1, 2, 3 and/or 4 during normal operation. This is consistent with the previously listed assumption in the exchanger network operation. The combination of all the algebraic equations in this section will easily allow us to simulate the heat exchanger network performance during all periods  $p$  of interest. The mentioned operational requirements above will serve to generate secondary constraints for this problem. Firstly, at least three heat exchangers out of the first four must always be in service due to momentum transfer requirements. This yields:

$$y_{1,p} + y_{2,p} + y_{3,p} + y_{4,p} \geq 3$$

Secondly, at least one of the last two heat exchangers must always be in service due to heat transfer requirements. This yields:

$$y_{5,p} + y_{6,p} \geq 1$$

Additionally, the outlet temperature of the system must be maintained under 93°C as per downstream process unit requirements:

$$\frac{y_{5,p} \cdot T_{5,p}^{h,out} + y_{6,p} \cdot T_{6,p}^{h,out}}{y_{5,p} + y_{6,p}} \leq 93$$

As a final constraint, it is a good idea to ensure that no single heat exchanger is cleaned in two consecutive periods. This is done using:

$$y_{n,p} + y_{n,p-1} \leq 1$$

Now that all the relevant constraints are defined, an acceptable objective function must be derived. From literature review, it is apparent that many academic leaders in the field of scheduling prefer to minimize operating cost as their objective. This makes conceptual sense and serves as our approach. The operating cost is comprised of two key components in this case: 1) Cost of Heat Exchanger Cleaning: This is a self-explanatory cost. As the heat exchanger is taken out of service, typically the contracting party doing the cleaning will require compensation for their services. 2) Cost of Energy (Heat) Losses due to Fouling: Fouling causes reduction in total heat exchanged during normal operation, and additionally forces the heat exchanger to be ultimately taken out of service. This means that relative to an ideal case without fouling, there is a substantial loss of potential heat transferred during normal and out-of-service heat exchanger states. In our case, the Cost of Energy is essentially the additional amount of glycol (in \$) required in HX E & F per unit drop in energy per heat exchanger. The objective function can be mathematically described as:

$$Total\ Cost = \sum_{p=1}^{P_{total}} \sum_{n=1}^6 (Q_{clean,n} - Q_{n,p}) y_{n,p} \cdot C_{energy} \cdot \Delta t + \sum_{p=1}^{P_{total}} \sum_{n=1}^6 C_{clean} (1 - y_{n,p})$$

where  $C_{energy}$  is the cost of unit energy and  $C_{clean}$  is the cost per cleaning. The combined model described in this section is solved on GAMS using DICOPT. This enabled the generation of a heuristic solution for this non-convex MINLP. Other solvers (which may have been more efficient) were not used for this project due to limited resources.

#### 4. Case study

Figure 4 illustrates the HEN under consideration for this project. The network and subsequent data are associated with a typical operating SAGD Facility. In essence, the produced water recovered from the thermal SAGD operation is to be cooled before entering the de-oiling and water treatment units. This water is cleaned and converted to steam before being injected back into the reservoir. There are 6 heat exchangers. The first set of four heat exchangers cool the produced water with de-oiled water (cross heat exchange to maximize heat transfer). The second set of heat exchangers (E & F) do the majority of the cooling using glycol as a cooling medium. All the heat exchangers are Shell & Tube type. Additionally, the following operational constraints apply to this network: 1) at any given time, three heat exchangers must be in service out of the first set of four (due to pressure drop constraints), 2) at any given time, one heat exchanger must be in service out of E & F (due to heat transfer requirements), 3) the outlet temperature of the Produced Water stream entering the Deoiling Unit must not exceed 93°C.

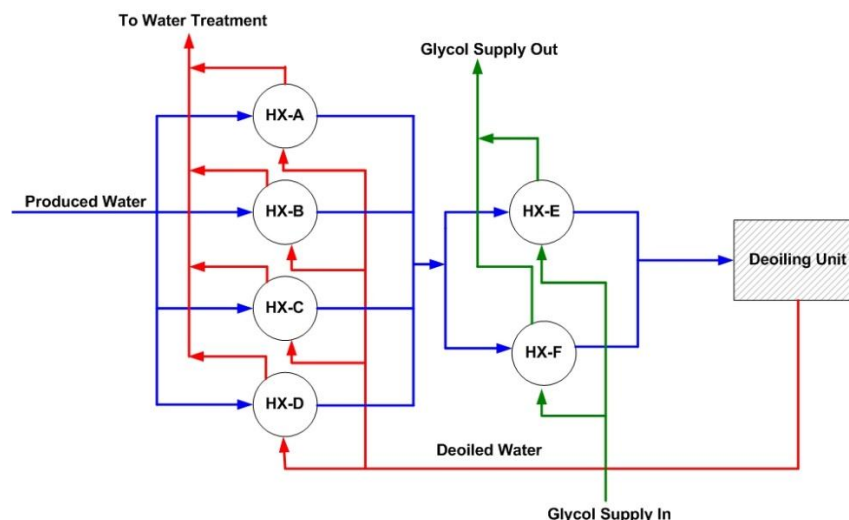


Figure 4. Process Flow Diagram of the Heat Exchanger Network under consideration. This is a very common network for Produced Water Cooling in many SAGD facilities in Canada.

## 5. Results and Discussion

### 5.1 Fouling and OHTC Calculations & Regression

From the methodology explained in the previous section, OHTC and fouling factor were calculated quite easily. Non-Linear Regression on certain runs was then conducted to fit the empirical exponential model. Statistical Analysis on the regression proved that it was in fact significant, and the  $R^2$  (a factor describing the residual sum of squares relative to total sum of squares) remained in an appreciable range. The regression parameters are displayed below.

Table 1. Empirical Model Parameters obtained from Non-Linear Regression Analysis of Operating Data

Heat Exchanger	Regression Parameters	
	$U_o$ (W/m <sup>2</sup> ·°C)	$k$ (hour <sup>-1</sup> )
A	303	0.05
B	225	0.04
C	263	0.04
D	485	0.04
E	2349	0.15
F	2215	0.16

There is obviously a notable difference between the parameters for A-D and E-F. This is because of the different size of the heat exchanger, as well as the different flow configurations. For instance, in A-D the produced water is on the Shell-Side whereas in E-F it is on the tube side. Consequently, the maximum available OHTC differ drastically. In addition, there is a significant difference between the maximum available OHTC between a combination of ABC and D. This is because D was only recently installed. This illustrates to a potential permanent decay of heat transfer in A, B or C, or simply preferential flow to D due to a lower overall pressure drop across this heat exchanger. These are important points but remain outside the scope of this project. Figures 5-10 illustrate several runs that were used to generate regression parameters for each heat exchanger. It is important to note that the runs utilized tend to closely mimic the operating conditions utilized during the optimization model.

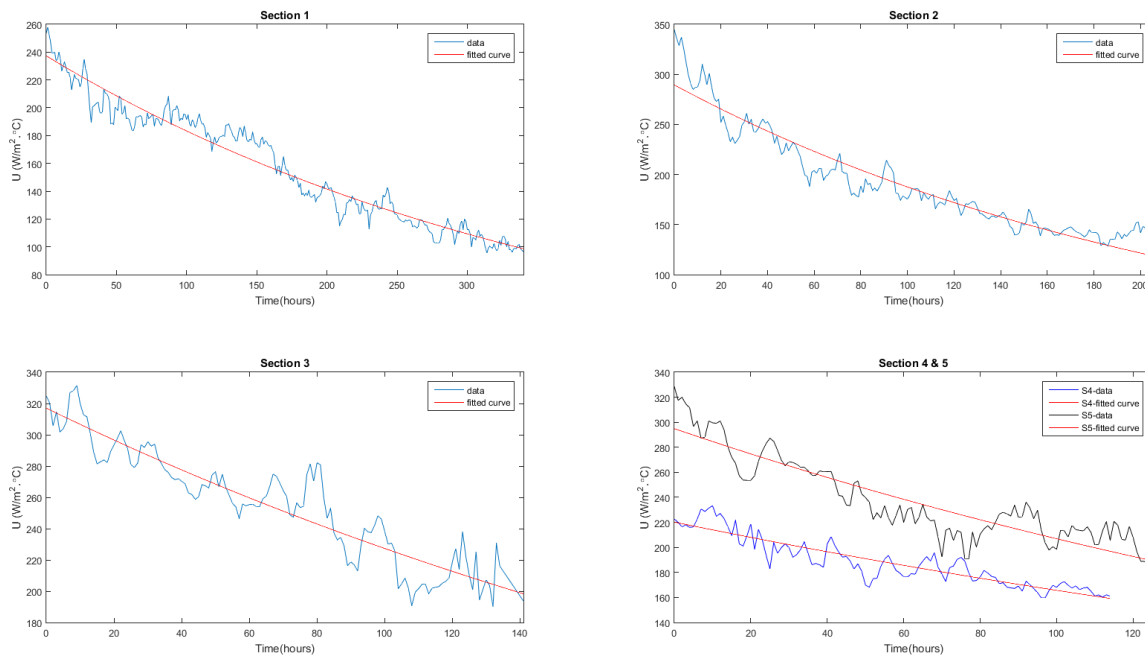


Figure 5. Runs utilized for OHTC Regression Analysis for Heat Exchanger A

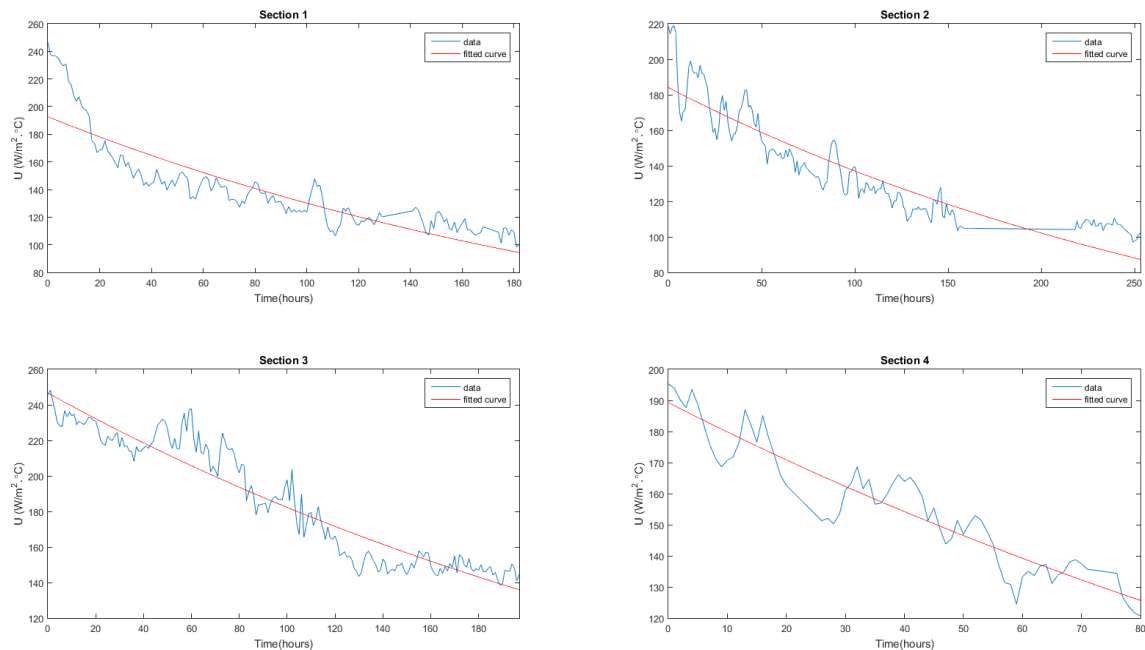


Figure 6. Runs utilized for OHTC Regression Analysis for Heat Exchanger B



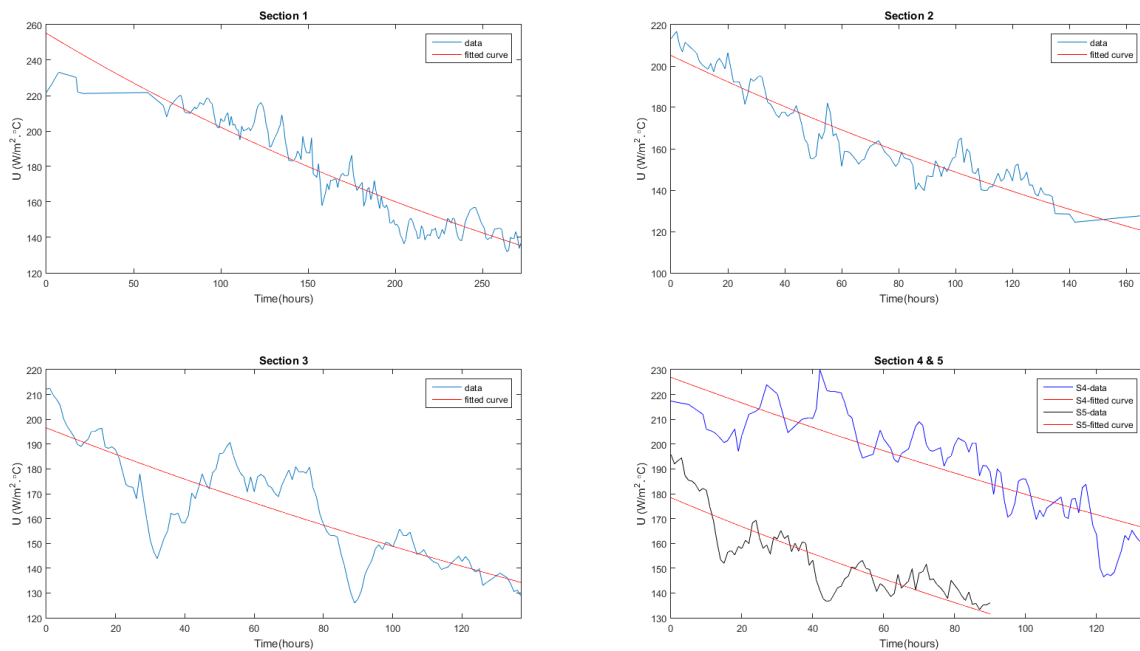


Figure 7. Runs utilized for OHTC Regression Analysis for Heat Exchanger C

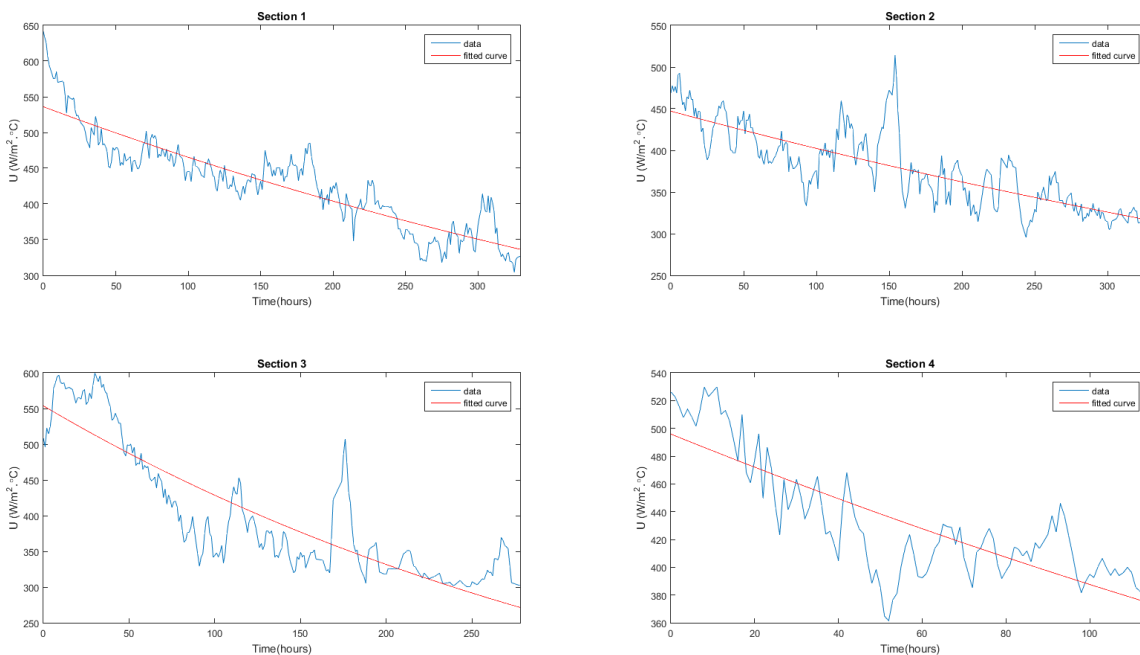


Figure 8. Runs utilized for OHTC Regression Analysis for Heat Exchanger D

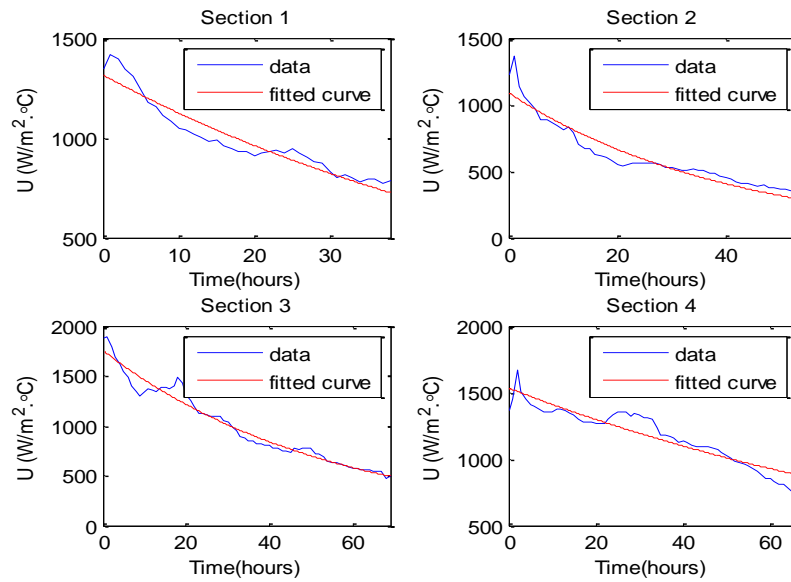


Figure 9. Runs utilized for OHTC Regression Analysis for Heat Exchanger E

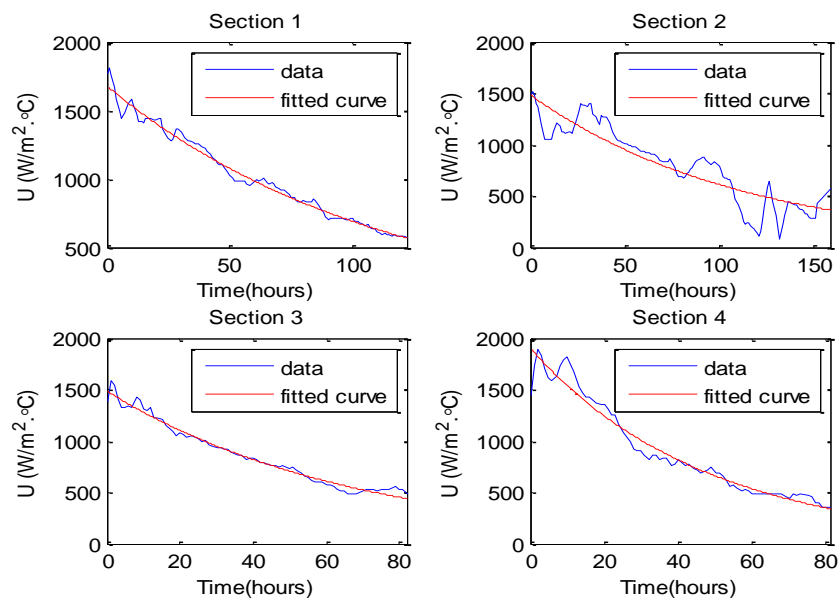


Figure 10. Runs utilized for OHTC Regression Analysis for Heat Exchanger F

## 5.2 Optimal Cleaning Schedule

The results from the previous section are inputted to the developed optimization model. The following deterministic operating conditions (close to design) are used during the case study:

Table 2. Deterministic Operating Conditions used in the Optimization Model

Operating Conditions	
Produced Water Volumetric Flow Rate (m <sup>3</sup> /day)	24,000

Produced Water Inlet Temperature (°C)	125
Glycol Inlet Temperature (°C)	30
Heat Transfer Area for HX - A to D (m <sup>2</sup> )	642
Heat Transfer Area for HX - E to F (m <sup>2</sup> )	732

The solution of the Optimization Model from GAMS was transpired to MatLab, from where it was written and collected in an Excel File. A visualization of the optimal cleaning schedule is described below.

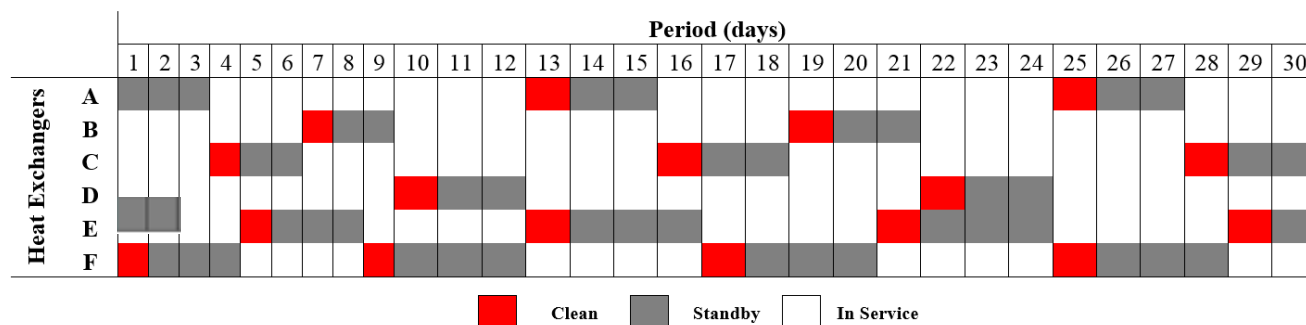


Figure 11. Optimal Cleaning Schedule for HEN under consideration

The schedule above essentially indicates a 9-day run time and 3-day offline time for HX A-D. As well, there is a 4-day run time and 4-day offline time for HX E-F. Notice, that the constraints in this problem essentially ensured that the feasible region was small. In fact, an iterative calculation by hand could have been conducted subject to the constraints to solve this particular problem. However, as the complexity of the constraints and networks grow, the optimization methodology will become exponentially more useful. A total of 16 cleanings are required for this schedule in a month. In the cleaning schedule provided by the facility, there were 18 scheduled cleanings. Thus, neglecting the additional energy savings, there is a direct saving from 2 less heat exchanger cleanings. This corresponds to a monthly savings of \$ 30'000.

The more correct number to compare would be a comparison of the total operating cost. However, the plant has an uncertain price for additional glycol supply which complicates this comparison. However, since we are cleaning more frequently in the optimal schedule, the energy losses suffered should be minimum and the overall operating cost will be drastically lower relative to original operating cost. The above schedule can be used to simulate the outlet temperature of Produced Water entering and exiting HX-E or HX-F (which ever one is in service). This is depicted below. Notice that all our constraints are met and the heuristic solution from DICOPT appears to indeed be very close to an optimal solution.

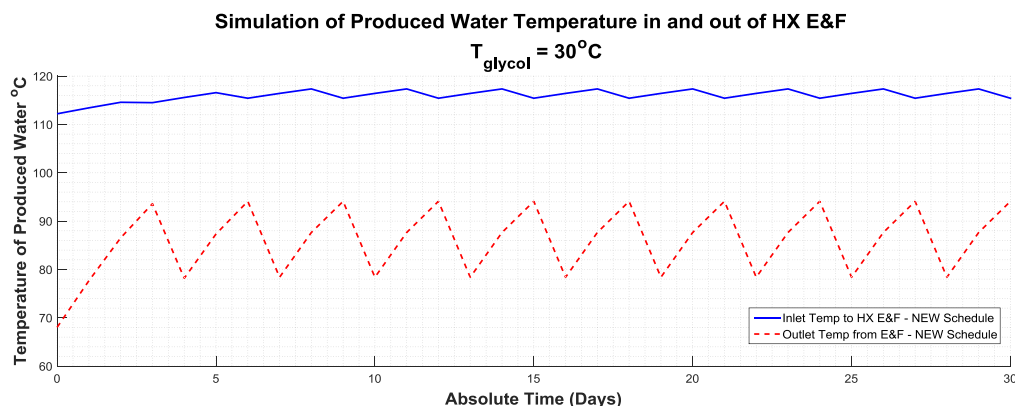


Figure 12. Simulated Outlet Temperature of the HEN (red) using the operating parameters listed above

## 6. Conclusions

In this study, it has been proven that a mathematical optimization approach can play a crucial role in minimizing operating cost incurred from heat exchanger operation. Many plants have sufficient operating process data to make data-driven scheduling decisions, backed by tested and proven optimization models. A savings of almost \$30'000/month is displayed from the use of such a scheme in the HEN considered throughout this project.

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