

# **Evolution of the Von Mises Stress of a Cracked Plate**

**Mokhtar .Bourdim and Siham.Kerrouz**

Relizane University Center Ahmed Zabana, ALGERIA

[mokhtar\\_61@yahoo.fr](mailto:mokhtar_61@yahoo.fr)

**Abdelghafour .Bourdim**

Mechanical Engineering Department University of Tlemcen, ALGERIA

[bourdim56@yahoo.fr](mailto:bourdim56@yahoo.fr)

## **Abstract**

To promote prevention must study the behavior of these structures in the case of accidents, as shocks to prolong the lifetime of the structures. To predict the dynamic behavior of structures under the impact effect, we addressed the dynamic problem as a modeling and a numerical resolution. Indeed, this work is part of the dynamic impact study on a cracked plate. Our choice focused on numerical simulations to examine the response of a cracked plate aluminum alloy impacted by a spherical projectile diameter of 40 mm. A comparison was made with the case of a healthy plate flawless dynamically biased in the same conditions.

## **Keywords**

Cracked plate, impact, dynamic, modeling, numerical simulation, aluminum alloy, projectile

## **1. INTRODUCTION**

The collision is the structural impact between two solids or other rigid obstacles affect the safety of some structures [1-5]. The dynamic analysis of cracked plates was performed by several authors. Some authors require previous knowledge of the impact force others involve as part of the problem [6] and suggest its determination at the same level with the resulting stresses, the arrow, the deformation...ect, [7- 12]. In this study we present the modeling and numerical simulation of impact dynamics of a rigid spherical projectile on a flexible plate cracked in order to see the evolution of the stress Von Mises.

The behavior of the plate when shock was analyzed in terms of stress and deformation. The influence of the crack size on the dynamic response of the plate was also discussed.

## **2. DIMENSIONS OF THE CRACKED PLATE AND THE PROJECTILE**

The table below summarizes the dimensions of the fissured plaque and the projectile

Table 1. Geometrical characteristics of the plate and projectile

Structure	Dimension
	Length $L = 400$ mm
Plate (target)	Width $l = 200$ mm
	Thickness $t = 3$ mm
Sphere (projectile)	Radius of the sphere $R = 20$ mm
Initial distance between the plate and the sphere	$d = 10$ mm

### 3. DYNAMIC DATA

The cracked plate is supposed flexible while the sphere is taken as a rigid form the data speed and duration of impact are the following[13]:

- 1) Speed of projectile  $v = 45\text{m/s}$ ,
- 2) Impact duration  $t = 0,02\text{s}$ .

The geometry of the cracked plate and the sphere is given by Figure 1 and Figure 2.

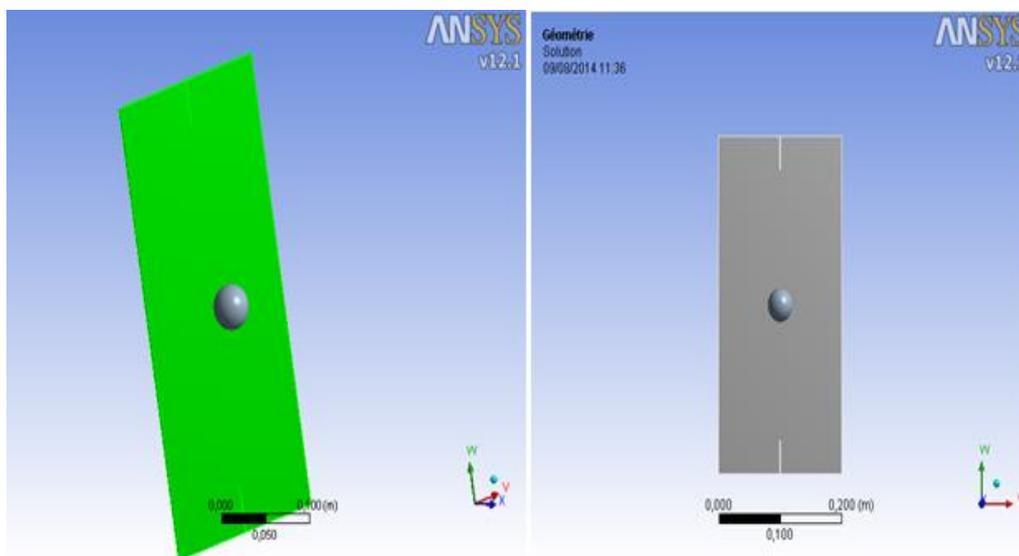


Figure 1. Geometry of the plate and the sphere.

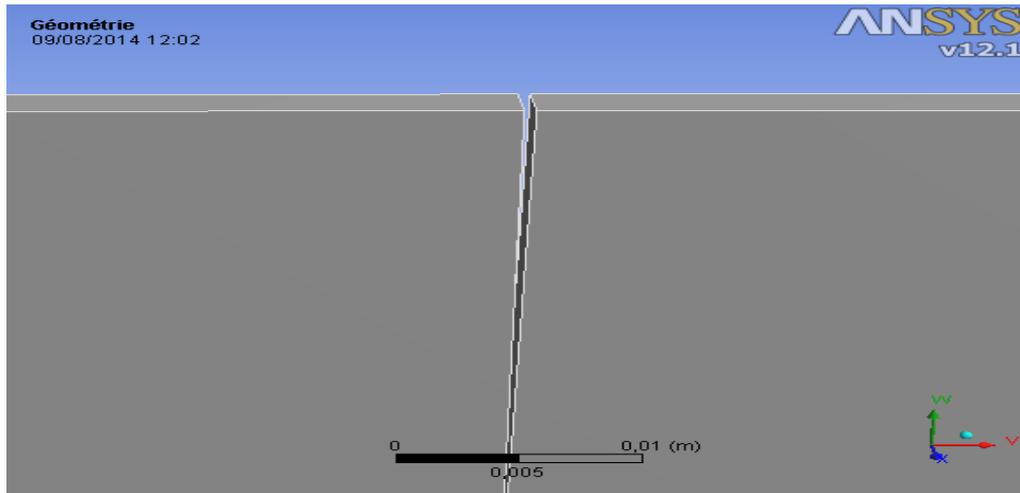


Figure 2. Geometry of the cracked.

#### 4. MECHANICAL CHARACTERISTICS OF THE CRACKED PLATE AND THE PROJECTILE

The mechanical characteristics of the cracked plate and the projectile are given in the following table (See table 2).

Table 2. Mechanical characteristics of the cracked plate and the projectile

Material	Density $\rho$ (kg/m <sup>3</sup> )	Young's modulus E (N/m <sup>2</sup> )	Poisson coefficient $\nu$	Mass m (kg)
Alloy aluminum plate	2770	7,1E +10	0,33	0,66463
Projectile in steel	7850	2E+11	0.3	0.263

#### 5. BEHAVIOR ANALYSIS OF THE CRACKED PLATE UNDER THE EFFECT OF THE IMPACT BY A SPHERICAL PROJECTILE

For modeling and numerical simulation of the effect of the projectile impact on the cracked plate, the code ANSYS (workbench) has been used. The boundary of conditions applied to the cracked plate is defined by a recess of two uncracked edges of the plate in Figure 3. The mesh of the cracked plate and the sphere are shown in Figure 4.

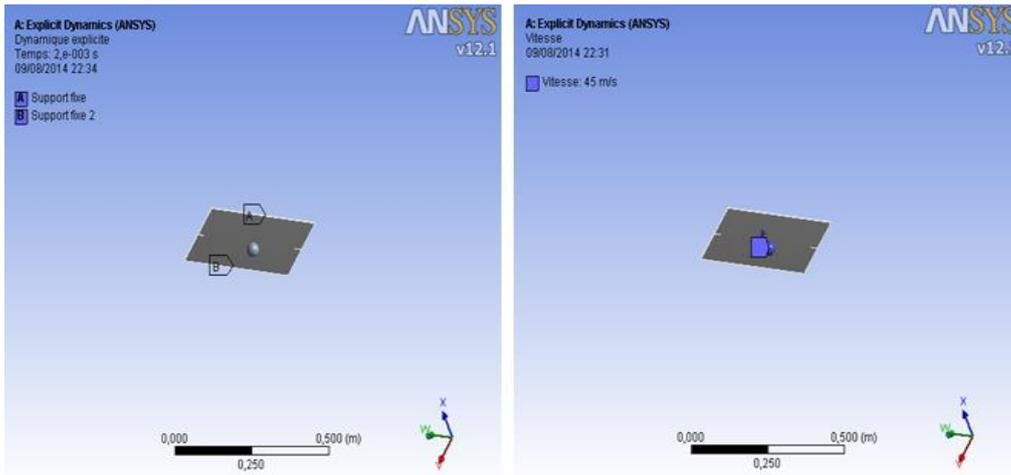


Figure 3. Boundary of conditions applied to the plate.

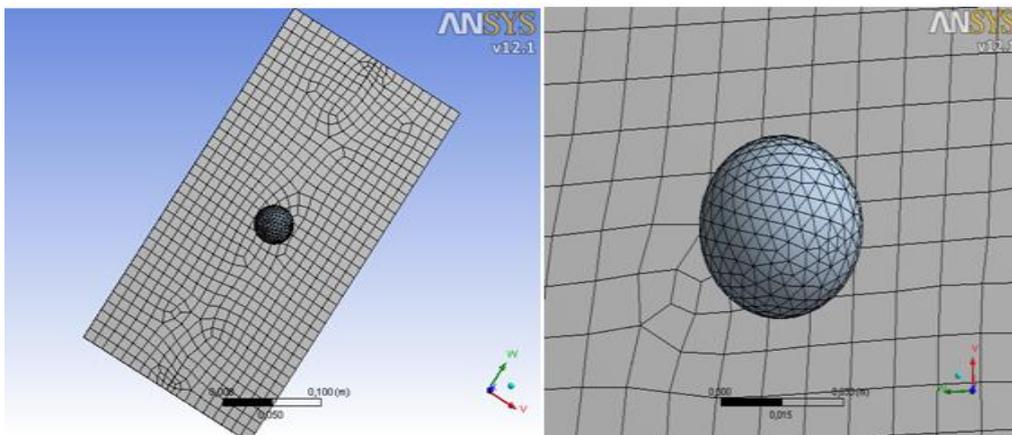
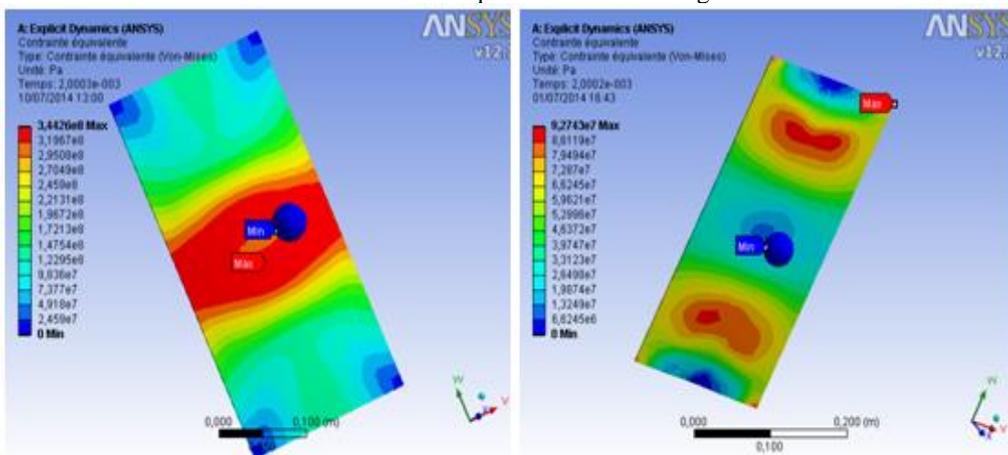


Figure 4. Mesh of the plate and the sphere.

## 6. RESULTS AND DISCUSSIONS

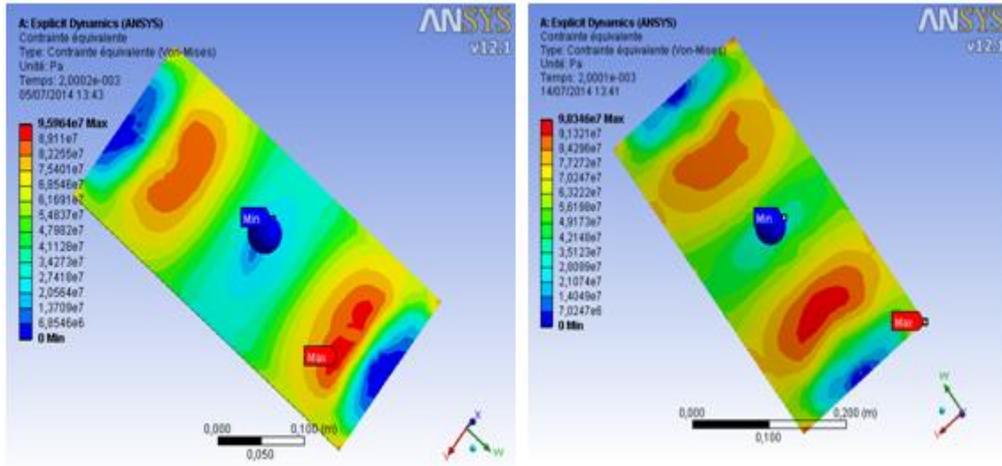
### 6.1 Constraints of Von Mises

The constraints of Von Mises at the moment of impact are shown in Figure 5.



(a) Equivalent stress  $a/w = 0$

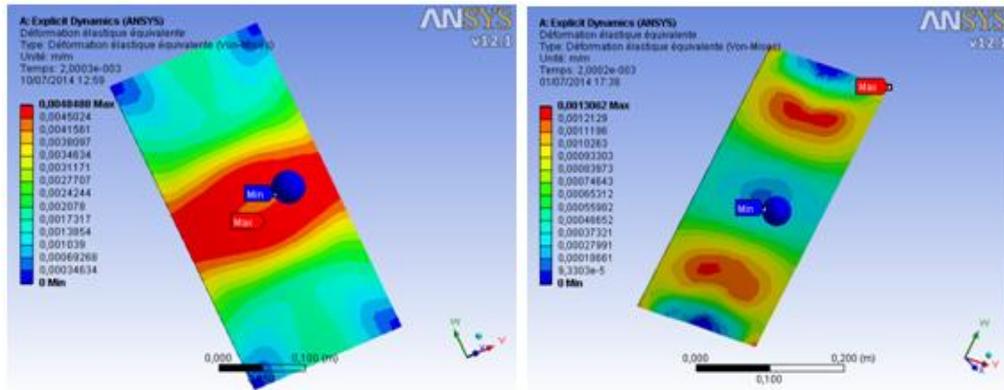
(b) Equivalent stress  $a/w = 0,063$



(c) Equivalent stress  $a/w = 0,075$

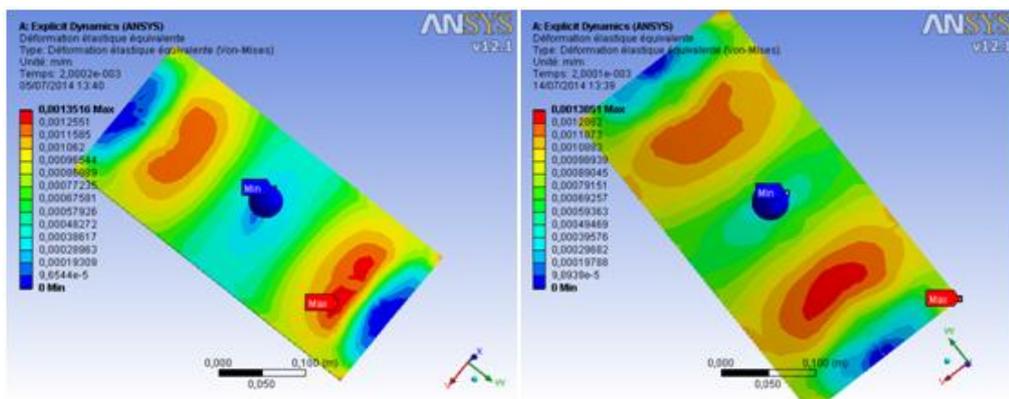
(d) Equivalent stress  $a/w = 0,1$

Figure 5. Constraint of Von Mises for an impact speed 45m/s and for different crack lengths.



(a) Equivalent elastic deformation  $a/w = 0$

(b) Equivalent elastic deformation  $a/w = 0,063$



(c) Equivalent elastic deformations  $a/w = 0,075$

(d) Equivalent elastic deformations  $a/w = 0,1$

Figure 6. Elastic deformations of Von Mises.

The figure 5 and figure 6, represent the constraint distribution along the cracked plate and the uncrack plate.

For the uncrack plate is embedded on both sides Fig. 6(a), we can deduce that the elastic constraint of Von Mises and the elastic deformation of Von Mises are highest around the point of contact and they gradually diminish to the corners of the edges of the plate.

For the three cracked plate figures 6(b), 6(c) and 6(d), it is found that the constraint field is maximum in the zone located near the tip of the crack then it decreases gradually as and when that one moves to the free edges of the crack. In addition, the constraints in the point are very weak. The constraint field is inversely proportional to the crack length.

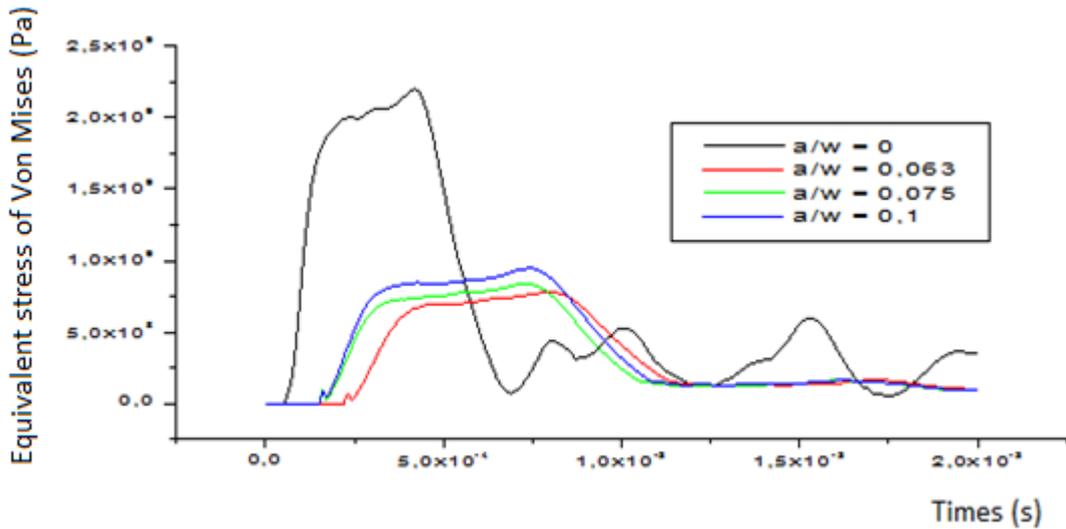


Figure 7. Evolution of the constraint of Von Mises versus time for an impact speed of 45m/s.

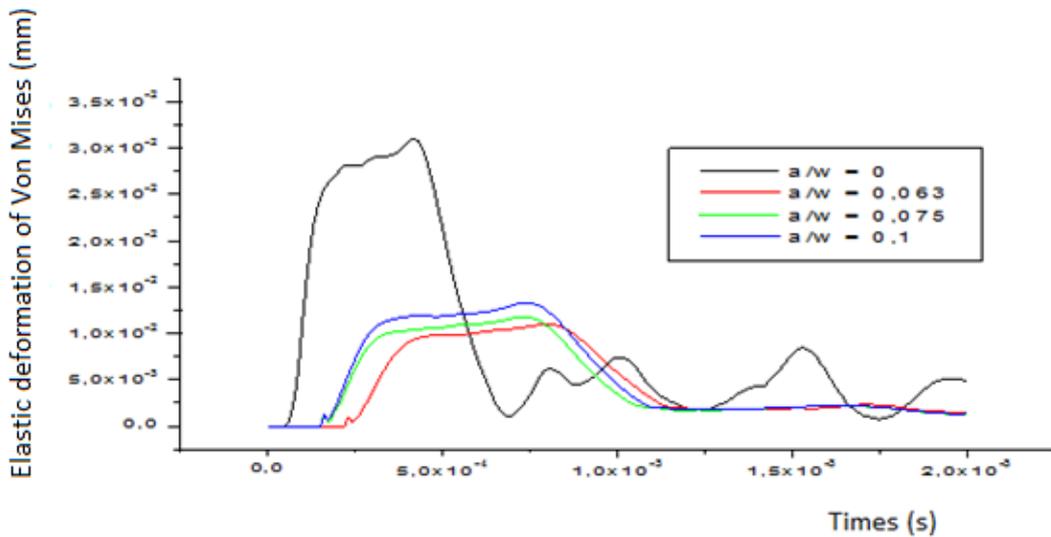


Figure 8. Evolution of the demonstration of Von Mises versus time for an impact speed of 45m/s. The figure 7 and Figure 8, represents that for the three cracked plates, the curves of elastic constraint and elastic deformations of Von Mises have the same paces and they pass through three phases, the first phase comprises two stages; the first stage correspond to the contact between the plate and the sphere, and the second one sees the level of constraints and the deformations arise with damage caused by the difference between potential energy and kinetic energy of the two structures (the energy of the impactor is greater than that of the plate). The second phase is when damage is present with peaks of constraints and deformations. The third phase is the damage where a portion of the energy used to make up the impactor, it is the phenomenon of the rebound.

## 7. CONCLUSION

The study allowed us to understand the behavior of a healthy plate and a cracked plate under the effect of a dynamic impact of spherical projectile types. It was found that the healthy plate had a higher dynamic behavior as that of an identical cracked plate at the edges. For the uncracked plate, at the moment of the impact, the deformations and the constraints are maximal around the contact point so for the cracked plate, these are highest in the vicinity of cracks peaks. Increasing the length of the edges of cracks has an influence on the dynamic behavior.

Of the cracked plate through the evolution of constraints and dynamic deformations.

## Acknowledgements

This work was supported by laboratory water and works in their environment (Laboratoire eau et ouvrages dans leur environnement EOLE).

## References

- Moriarty, G., A. Poursartip., *Technology and Engineering In the impact test the velocity history during impact*, Ken Street, 1995.
- Minak, G., Ghelli, D., *Influence of diameter and boundary conditions on low velocity impact response of CFRP circular laminated plates*, Part B. 39, pp. 962-972, 2008.
- ELNASRI, I., Comportement des matériaux cellulaires sous impact et de panneaux sandwichs sous perforation dynamique, *Thèse de doctorat de l'école normale supérieure de Cachan*, France 2006.
- Craven, R., Sztefek, P. and Olsson, R., Investigation of impact damage in multi-directional tape laminates and its effect on local tensile stiffness, *Composites Science and Technology*, Vol. 68, pp. 2518-2525, 2008.
- Ladeveze, P., Allix, O., Deü, J.F. and Léveque, D., A mesomodel for localization and damage computation in laminates, *Computer Methods Application Mechanical Engineering* 183, pp. 105-122, 2000.
- Muskhelishvili, N.I., Some basic Problems of mathematical theory of Elasticity, *English translation*, Noordhoff, 1957.
- Freund, L.B., Rice, J.R., On the determination of elastodynamic crack tip stress field, *International Journal Solids Structure*, Vol. 4, pp. 293-299, 1974.
- Russel, C., Mechanics of Materials laboratory, *Simon and Schuster Childrens*, 2000.
- Espinosa, C., Collombet, F., Impact de plaques composites, caractérisation et modèles, *Laboratoire de Mécanique-Physique*, U.R.A. C.N.R.S. N 867, Université de Bordeaux I, 1991.
- Lin, C., HooFatt M.S., Perforation of composite plates and sandwich panels under quasi-static and projectile loading, *Journal of Composite Materials*, Vol. 40, pp. 175-190, 2006.
- KUJAWSKI, D., Estimations of stress intensity factors for small cracks at notches, *Fatigue Fract Engineering Materials and Structures*, Vol. 14, pp. 953-965, 1991.
- Nillsson, F., A note on the stress-singularity at a non uniformly moving crack tip, *Journal of Elasticity*, Vol.4, pp. 73-75, 1974.
- SIH, G.C., Dynamic aspects of crack propagation, *Inelastic Behaviour of Solids*, Eds Jaffe R.I, pp. 607-634, 1970.
- Kerrouz, S., Etude dynamique d'impact sur une plaque fissurée, *Thèse de Magister Université d'Oran Algérie*, 2015.

## Biography

**Bourdim Mokhtar** is currently a fulltime senior lecturer and Head of Mechanical Engineering Department at Relizane University Ahmed Zabana in Algeria, holds a Bachelor of Science degree, a Master and a Phd in manufacturing process from Higher National School of Education Oran in Algeria.

**Bourdim Abdelghafour** is Senior Lecturer and Head of Industrial Maintenance Master in Mechanical Engineering Department at the Faculty of Technology at the University of Tlemcen in Algeria. He earned B.S. in Mechanical Engineering from University of Ottawa in Canada, Masters in Mechanical manufacturing from University of Science And Technology of Oran in Algeria and PhD in Industrial Engineering from School of Arts and Crafts (Ecole des arts et métiers) in Lille -France. He has published journal and conference papers. He was responsible for several research projects in strategy and industrial

maintenance management. His research interests include manufacturing, simulation, machine-tools dynamic.

**Kerrouz Siham** is a PhD student at the University of Oran Algeria and temporary university teaching center relizane Ahmed Zabana in Algeria