

# The digital twin model of vehicle containers to provide an ergonomic handling mechanism

**Ahmed M. Abed**

Associate prof. at Industrial Engineering Department,  
Zagazig University,  
Egypt, P.O.Box44519,  
[Ahmed-abed@zu.edu.eg](mailto:Ahmed-abed@zu.edu.eg)

**Samia Elattar**

Associate prof. at Department of Industrial & Systems Engineering,  
College of Engineering, Princess Nourah bint Abdulrahman University,  
P.O.Box84428, Riyadh 11671, Saudi Arabia.  
[SAElattar@pnu.edu.sa](mailto:SAElattar@pnu.edu.sa)

**Tamer S. Gaafar**

Assistant prof. at Computer and Systems Department,  
Zagazig University  
Egypt, P.O.Box44519.  
[tsgaafar@zu.edu.eg](mailto:tsgaafar@zu.edu.eg)

## Abstract

Late order loss for difficulty handling (loading and unloading) activities left an alarm message to make traditional transportation handling for distribution e-commerce more accessible through mitigating it to semi-auto actions. This article discusses the idea of Vehicle Containers made up of Permutational Drawers, i.e., VCPD, that ensure ergonomic handling. The proposed Ergonomic Digital Twin (EDT) manages the VCPD by the Internet of things, i.e., IoT. The VCPD object has two dimensions: drawers' size and motion mechanism. These targets are implemented via establishing the digital twins' model, i.e., DT, for these drawers to test its qualifying for implementation, mainly if supported by IoT. There is still much confusion regarding the DT and how it will apply to the VCPD in medium-sized schemes for transportation enterprises. This work activates the IoT to bolster and simplify transportation activities through designing VCPD and control via a unified framework having several standard steps to reduce execution time, effort, and transportation costs.

## Keywords

Digital twin, IoT, Ergonomic Design, Mechanism design, and Container Repositioning.

## 1. Introduction, Digital Twins in transportation

The article hopes that digitalizing all transportation activities via the smart sensors platforms enhances the M2M interaction relationship. Digitalization must be aided by several recent technologies such as the Industrial Internet of Things (IIoT), artificial intelligence (AI), machine learning, and cloud computing (Ahmed M. Abed, 2020). Many researchers unanimously agree that a digital twin, an electronic replica of an organism, machine, parts thereof, or service (e.g., transportation is a service based on the organism) has four vertices (stakeholders, product, mechanism, and operator).

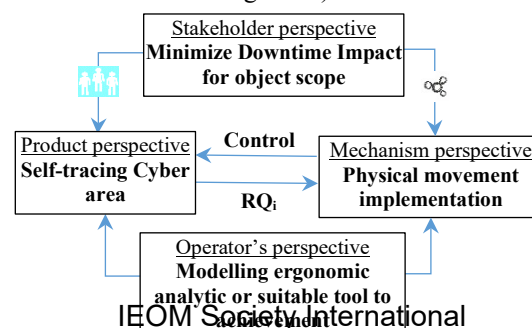


Figure 1. The bypass in bi-direction

and operators), with keep that the actual object/product (i.e., drawers) is connected to its virtual electronic version in an exceedingly way that permits data to be transferred between both mutually periodically (i.e., to modify the design (e.g., size, the weight of contents, empty spaces) according to stowage map, which interested with returned products). In line with a recent Gartner and researchers poll., 2019, which revealed 75% of enterprises are using IoT via designing digital twins to manage overall activities within the subsequent year. Over two-thirds of those businesses are expected to own a minimum of one digital twin aspect in their outputs by 2022 (Gartner, 2019), which can address by digitizing their operations, service mentality, and marketing acceleration. The digital twins were defined initially in 2002 (Grieves and Vickers, 2016) as "Digital info-media construction of a physical system as a single entity." began from a basic conceptual model of the product (i.e., drawer) life cycle management (PLM) to the term 'twin,' which refers to the fact that will link these digital data to the physical while incomplete existence, this think may enhance the closed stakeholders' chain cycle. Using this approach in transportation, which pushes the operators to develop workable digitization of all entities in their transportation schemes (e.g., from source to destination), via with analysis, decision-making, and control in agreeing to rules as illustrated in Figure-1, that means interactive bypass in two directions as illustrates in Figure-1.

The purpose of this study is to integrate these paradigms on the digital twin to derive a unified structure (i.e., domain) that allows industrialists to construct their digital twins to achieve specific goals readily through achieving five requirements as shown in Figure-2, inexpensively, and fast as has been deduced a standard and technology roadmap (Hedberg T Jr., Helu M, Sprock T., 2018), also tackling the Product lifecycle management (Grieves M., 2005) who put the basics of digital twins' concept and implementation. The Digital twin does well in facilitating corrective acts and predicts faults/fatigue even before they occur (i.e., over-processing/ergonomic issues). This interactive relation of EDT allows any physical object to interact with each other and with humans to enhance this relationship. The EDT is the true incarnation of implementing the Internet of Things, i.e., EDT=> VCPD & IoT, as pointed to Ahmed M. Abed, 2016, and Haag, S. and Anderl, R., 2018, who designed their framework mutually allows data flow is bidirectional.

### 1.1 Objectives

The main objective of the research is to define a simple guide to activate the digital twin in industrial operations and study their effectiveness. Also, it proposes some acceleration steps in transportation activities (i.e., vehicle routing consuming time) to create an ergonomic system that leads to customers satisfaction who get the goods early.

## 2. The Digital Twin establishing

Some researchers have recognized that the real-time visualization of closed control schemes to need decisions is also a vital step with digital twins than a disjointed virtual replica of a physical system such as illustrated in Figure-2, which consider the digital twin structure via meet the five requirements demonstrated in Figure-2. Table-1 discusses the Figure-2 elements and shows its definitions, relevant target standpoints (i.e., physical object, products, process, or service), the fidelity of digital acting (i.e., completed, or partial exemplification), and chronological interdependence (e.g., on or offline) (DUBLIN, 2020). Alternatively, an offline digital twin would attach to a commonplace's physical system. The difference between an offline digital twin and an emulation model is the periodic link, as discussed by (GE., 2018).

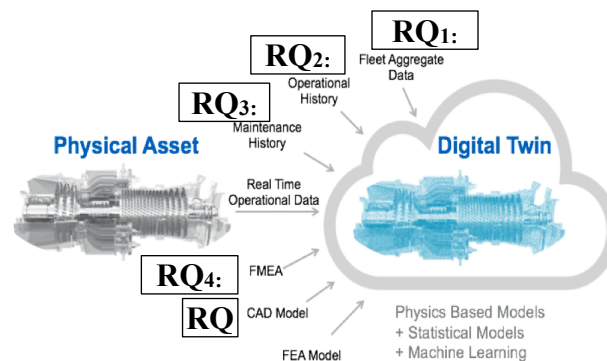


Figure 2. Source: (DUBLIN, 2020), Illustrative digital twin example

Table 1. RQ<sub>i</sub>; A Compilation of Different Standpoints on the Ergonomics' Digital Twin (EDT)

Reference	RQ <sub>1</sub> , Familiarization	RQ <sub>1</sub> , Fleet aggregate data	RQ <sub>2</sub> &3, Standpoint	RQ <sub>4</sub> , Fidelity	RQ <sub>5</sub> , CAD model
GE. 2018	Software representation	Offline	Product, Process	Completed	Yes
Siemens (2018) and also, Ahmed M. Abed (2020)	Virtual counterpart or computerized	On/Off-line	Product, Process, and Service	Completed	Yes
Siboni (2020)	Fully completed model	Online	Process, service	Piecemeal	None
Tao and Zhang (2017)	Authority model	Offline	Product	Completed	Yes
Coronado et al. (2019)	Digitized model	Offline	Service	Completed	Yes
Ahuett-Garza, (2018)	web-based system	Online	Service	Piecemeal	None
Bao, J., et al. (2019), Kritzinger et al., (2018)	Cyber counterpart or computerized	Online	Service	Piecemeal	None
Ahmed M. Abed et al., (2020)	Data and model	Online	Process	Completed	Yes
Boschert and Rosen (2016)	manifestos and paradigm	On/Off-line	Product, Process, Service	Piecemeal	None
Islam et al. (2020)	Digitized representation	Offline	Product	Completed	Yes

By extrapolating from Table 1, a digital twin shouldn't collect all accessible data from the real world, but only the knowledge relevant to the particular use case (i.e., vehicle's container accessing). Likewise, there should not be one digital twin for a physical paradigm. Still, a spread of DTs that support their intended serves to avoid the high expenditure (Berti, J.G., 2019). At the same time, the purpose of the standpoint model is assumed to be system (i.e., manipulation service). The study defines the system as digitizing, cyber, or computerized counterpart (Eckhart, M. et al., 2019).

Moreover, the study determines the degree of fidelity (completed) and the indicator of temporal integration in real-time or offline as discussed and reviewed (Grievies M. et al., 2016). The analysis concluded by developing the approach of Bolton D. 2016. Siemens et al., 2018 and updating Ahmed. M. Abed et al., 2020.

### 3. The proposed EDT framework entities

The EDT integrates the VCPD and IoT through three main criteria modify the outlines of the needed framework, which may influence the breadth and limits of a digital twin model:

**3.1. RQ<sub>1</sub>, [DTA] Fleet aggregate data:** The digital twin's models require online or offline updating according to service requirements during the time frame. The performance of EDT measures saves service time and likewise reduces the danger of fatigue. Additionally, the fidelity in supporting the transportation activities such as unloading or receiving returned items to placing them in the empty spaces. Therefore, should determine:

**3.1.1. Familiarization of the expected goals:** To determine the hopeful design (drawers' dimension and motion mechanism), the authors wish to define the design requirements precisely through step-by-step pictorial monitoring for actual operational activities. Generate this design needs digital sensors for aggregating data about the products weights, volumetric dimensions, empty spaces, which has turn access on by many trips at various destinations. This design is managed through IoT via “RQ<sub>1</sub>, fleet aggregate data.” and requires familiarization with the appropriate hardware's need next.

*3.1.1.1. The device connectivity and data format* cover how sensors and actuators communicate with legacy devices in EDT, the raw format of datasets created by machines, how devices communicate with the edge layer (e.g., PLCs and RTUs) in local EDT. While, activate the protocol translation between devices and gateway using the telemetry schemes based on BAC-net and Modbus such as eco-design Bluetooth, Z-Wave, ZigBee, Wi-Fi, Ethernet, and Serial Port, to feed the sensors to meet **RQ<sub>1</sub>**.

3.1.1.2. *Identify the PACE's sensors*; It must meticulously identify hardware, equipment, and machinery to urge appropriate suitable sensors needed to link them to the designed platform, counting on the organization goals and desired outcomes through the period of “operational history” to meet **RQ<sub>2</sub>**.

**3.2. RQ<sub>3</sub>, [DTI] Standpoint:** The standpoint determines whether development is needed via studying “the maintenance capability/reliability of operation history.” Then selects suitable mechanism wanted, such as if the digitizing twin will mimic the historical behavior of the paradigm (i.e., emulation) or if it will establish a dynamic model express the paradigm, i.e., simulation, (Brooks B. et al., 2014). Therefore, we should prepare the data points and metrics.

**3.2.1.** Preparation of data points and benchmarks consistent with results is a good step generated by the sensors attached to the cloud devices, resulting in enormous datasets. Therefore, it's critical to pick or guide the appropriate data points to contribute to the metrics. These points define the connectivity tactic that should be designated the device connectivity (**RQ<sub>1</sub>** and **RQ<sub>3</sub>**).

**3.2.2.** The setting needed to support a standpoint determines how data is saved before transferring to the IoT platform. Also, ensure the edge layer that must convert the transfer protocol to wireless protocols to provide the digital twin (e.g., CSV to XML to JSON).

**3.2.3.** Identify authority datasets required for transforming sensor data; when the correct setting is provided to the datasets collected by sensors and devices, they become relevant.

**3.3. RQ<sub>3.1</sub>, Accessibility,** is crucial for the Digital twins' model, which is supported with IoT, as a Clouds computing initiative via the platform as well discussed in Table-2 later, which must be carefully anonymized, encrypted, and compressed to transfer acceleration through intelligence dashboards as discussed in bullets 1, and 2 of this section.

**3.3.1. Identify hot path analytics for near-real-time treatment;**

single data points (i.e., traditional EDT) must be reviewed as they are generated, as aforementioned. After detecting unexpected indicators of arguments restrictions, the IoT platform may be too late to take a suitable decision.

The digital twins' platforms illustrate in Table-2 a set of components that help prepare and manage Internet-related devices in real-time. One person, DTA, can collect data remotely from the system DTIs, control, and manage all Internet-related devices DTP, as noted by Grieves, M., 2014. The study prefers to use a platform that supports device managers and adopts any data collection methods convention. The target for analysis indicator should be done in real-time and supports a visualization policy, as noted by Berti, J.G. and Deluca, LS, 2019. Therefore, the study selects the Kaa IoT platform to digitize the traditional EDT to create an EDT framework (Table 2).

Table 2. Comparison for open-source Internet platforms

IoT software platform	Do sets manage?	Strengthened	Basic Authentication	Data aggregation charter	Assay	Visualization support?	DataBase
Kaa IoT Platform	Yes	Mobile SDK is available to integrate any given platform, REST API	Link Encryption (SSL), RSA key 4096 bits, AES key 512 bits	MQTT, CoAP, XMPP, TCP, HTTP	Analyze and visualize IoT bi-data in-time Kaa Apache, Cassandra-Apache, Zappelin	Aye	MongoDB, Cassandra, Hadoop, Oracle NoSQL
DeviceHive	*Unknown	REST-AP, MQTT APIs	Basic Authentication using JSON Web Tokens (JWT)	REST API, WebSockets, or MQTT	Online analytics (Apache Spark)	Aye	PostgreSQL, SAP Hana DB
Thingsboard.io	Yes	REST APIs	Basic	MQTT, CoAP,	Real-time	No	Cassandra

			Authentication	and HTTP	analytics (Apache Spark, Kafka)		
WSO2	Yes	REST APIs	Link Encryption (SSL) and basic Authentication	HTTP, WSO2 ESB, MQTT	Yes, WSO2 Datum Analytics Server	Aye	Oracle, PostgreSQL, MySQL, or MS SQL

### 3.2.2 Define paths for batch processing

The framework classifies the sensors' data collection into two types, hot, i.e., indicators must be collected now, and cold, i.e., may be processed later, which is considered an essential part of developing an IoT solution as Grieves, M. and Vickers, J., 2017. This article adopts Kaa IoT to support the visualization in real-time through the open database.

### 3.4. RQ4, [DTP] The Expected Benefits of EDT framework and its needs.

At all levels of transportation, a DT of stakeholders, products, processes, or service/regime can be employed in various ways (e.g., M/c, cell, line, annex-facilities, or supply-chain).

a) *Minimizing the impact of mechanism downtime:* Therefore, the framework should be “self-tracing and repairing twin” via the monitor, troubleshoot, diagnose, and predict transportation equipment/devices faults and/or faults/fatigue to control the equipment. The preferred method in this setting is FMEA. The failure mode and effect analysis is based on the RPN risk priority number of multiply severity, occurrences/probability, and detection as shown in Table-3 and digitized as shown in Figure-3, and start the development from the maximum RPN. The ‘RQ4.i’ is divided to process, system, service, and software FMEA, as shown in Figure 4.

Table 3. The part of FMEA to develop the twin behaviour

Item / Function	Potential Failure Mode(s)	Potential Effect(s) of Failure	Severity	Potential Cause(s)/ Mechanism(s) of Failure	Probability	Current Design Controls	Detection	RPN	Recommended Action(s)	Responsibility & Target Completion Date
Customer sends in a quote request for product.	System, Software, Integration and Shipping requirements overlooked by	Customer needs not fully met by delivered system.	7	Human error	1	Design configuration tool.	3	21	Use configuration tool when available.	Closed 10/31/21

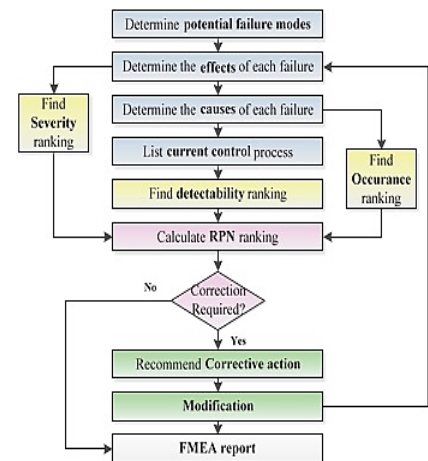


Figure 3. RQ4, FMEA Process to develop the object's twin

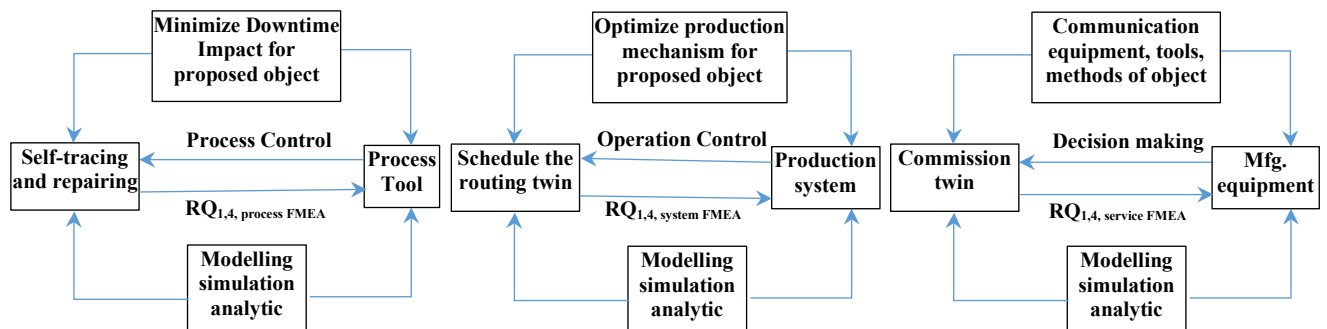


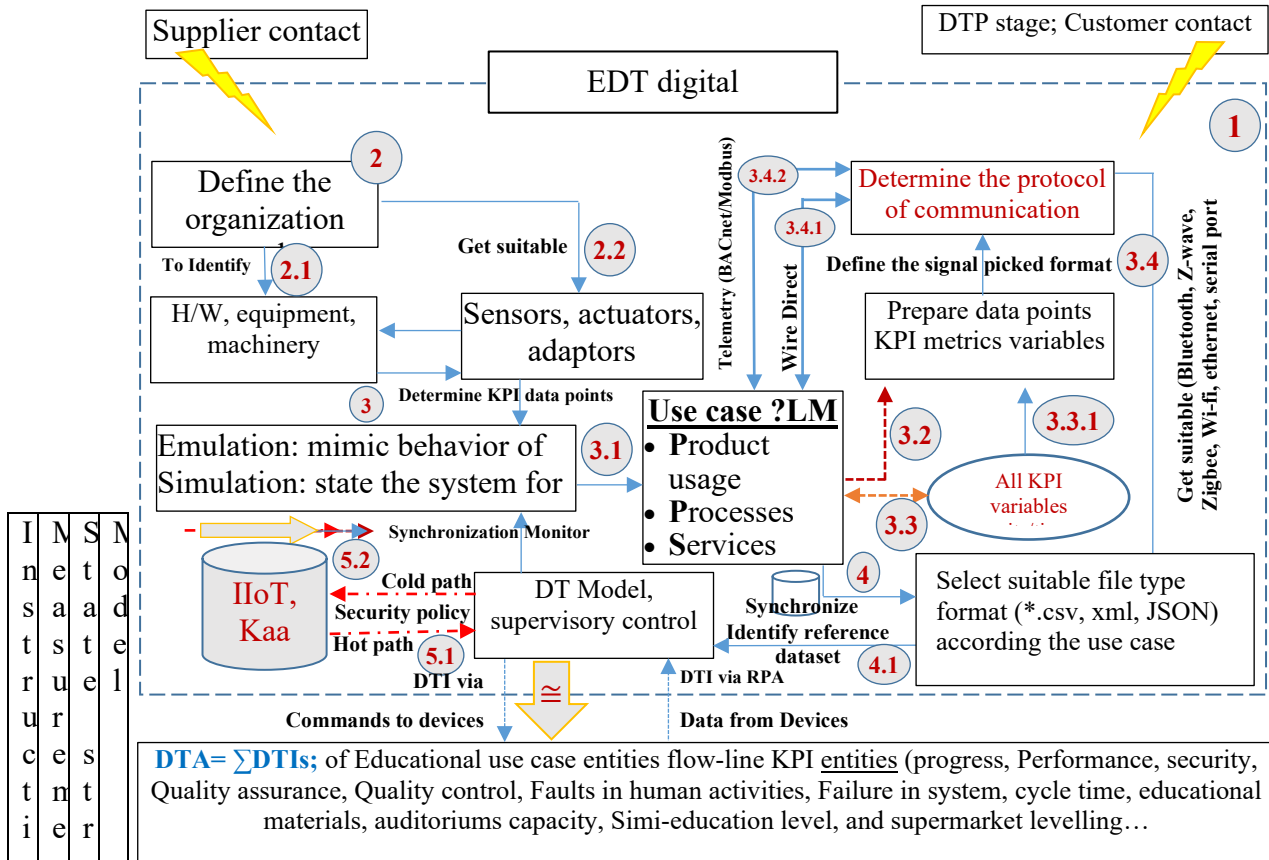
Figure 4. Depicts three cases of the use of DT in transportation sequence

#### 4. The EDT domain structure

The EDT is a computer-controllable system that will recommend future work through transportation 4.0 approaches to minimize fatigue, as shown in Figure-4 of the core components of traditional EDTs—changed by replacing. It is shown. The DT integrates real protests' characteristics, conditions, and behavior using case models through information tracing. Haag, S., and Anderl, R. It are based intensively on the declaration by the partner by 2018. Figure-5 shows the coverage of the entire system along with the process and product lifecycle. Given the design, prototyping, test policy, training, and virtual versions of analog for this cycle, digitization can help eliminate difficulties by making precise assumptions, which will help achieve “self-reliant reform and repair.” Ahmed M. Abed et al., 2020. In addition to talking about how the Digital Twin relates to Schemes Engineering and how it may help rectify "normal accidents" caused by human interactions as understand from Roberto. et al., 2022.

While Talkhestani, BA et al. (2018, 2019) and Coronado PDU et al., 2018 suggested integrating a PLM IT-Platform and a fulcrum (i.e., the data generated by multidisciplinary engineering tools) technique for detecting the mechatronic data structure discrepancies between digital models and physical schemes. Therefore, use automation software code to create a rule-based consistency checking and syncing the architecture models as noted by (Guodong, 2020). The proposed in the setting of transportation an approach of modeling and operational strategy. Firstly, the notion and expansion of the DT in the vehicle are detailed to give the implementation techniques of virtual-physical confluence and knowledge integration for a factory. Secondly, the modeling techniques for product, process, and operation digital twins are provided, followed by an explanation of the interoperation mode between these DTs. Thirdly, for modeling a structural parts machining cell, Automation Markup Language (Automation ML) is utilized to detail how to perform required activities, as shown in Figure-4. Finally, a performance evaluation illustrates how the suggested technique improves outputs efficiency. Therefore, Schleich, B., et al., 2017, and Zipper, H. and Diedrich, C., 2019 study proposes a strategy that uses optimization approaches to synchronize the states of the updating the model with those of the physical asset throughout outputs while also assisting in the detection and identification of changes. This stage is used to update a "double digital" version of the device's state in actual and real-time, called a "shadow device" used to develop the concept of a DT as cited by Ahmed M. Abed et al., 2020. The maestro of managing and updating the created twins is the IIoT dataset, which training some data at the cold path while synchronizing another influence data at a hot track to achieve fidelity situation, which the feedback and feed-forward flow across IIoT lifecycle phases (such as design and service) as shown in Figure-4, that contribute the vision 2030. At the same time, Eckhart, M., and Ekelhart, A., 2018, recreating CPS states based on properties only, needed for a wide range of security and safety measures.

The article presents an actual prototype implementation and assesses it in an experimental CPS test environment to demonstrate the viability of the specification-based state replication technique. The findings of Ekelhart, A., and the study indicate that attacks against CPSs may be successfully identified using the suggested state replication technique. The proposed ergonomic digital vehicle's container twin EDT developed the workplace as part of robotic process automation (RPA) as indicated in the proposed framework shown in Figure-5. The architecture of an EDT needs components enabling use cases like plug-and-play, self-x, and predictive corrective. Sundry procedures, including the Anchor-Point-Method, a method for diverse data gain and data unification, and an agent-based approach to progress a co-imitation (i.e., simulation) between EDT entities. The proposed framework respects the stages of modeling EDT twins (i.e., DTP, DTI, and DTA). The DTP considers designs, analyses, and processes paths to realize competitive transportation activities. Whereas a DTI is the digital access purpose of each equivalent of stakeholders, through its serial transportation processes'. While, the DTA could be a compilation of DTIs whose information and knowledge will be used to question academic progress, predictions, and learning. DTs' specific information is derived according to use cases (Gottfried Hastermann, 2021). With increasing numbers within the transportation processes, the opportunities for higher productivity are gap up. Therefore, the framework of the long-run industrialization results in four aspects: stereotyping, independence, communication, and digital schemes twin. The framework perceives a new method to optimize customer level, lessen variances, and assist with root-motive analysis. Finally, connectivity, just like the Internet, makes it feasible to narrow the gap of the digitization loop via the aid of online use. The proposed framework aims at increasing customer satisfaction, especially when monitoring, diagnosing, and predicting them, to improve asset performance and use based on DUBLIN, 2020 vision. In this setting, sensory data can be combined with significant data, human and fleet experience, and simulation learning to improve the results of predictions as recommended at ASME 2021 [36]. Therefore, complex forecasting platforms and an innovative corrective system can use DTs to find the underlying cause of problems and enhance outputs as recommended by Alberto, 2022. This stage precludes predictive corrective for its ability to forecast and identify variances for individual equipment or transportation processes that indicate the need for preventative repairs or corrective before a serious problem occurs.



<b>User Entity</b>						Data translation FE	Data Assurance FE	Security Support FE	Cross system Entity
<b>User interface FE</b>									
<b>Core Entity</b>									
Operating and administrating sub-Entity		App. and favor sub-Entity		Access and sharing of resources between the sub-entity					
Digital Modelling FE	Corrective FE	Simulation FE	Reporting FE	Interoperability support FE	Plug and Play Support				
Presentation and representation FE	Synchronization FE	Analytic service FE	Application Support FE	Access control FE	Peer interface FE				
<b>Data aggregation and appliances control Entity</b>									
Data aggregation sub-entity			appliances control sub-entity						
Data collection FE	Data preprocessing FE	Identification FE	Controlling FE	Actuation FE	Identification FE				
<b>Observable Transportation Elements</b>									
<b>Resource specific FEs</b>									

Figure 5. The EDT framework to manage digitized vehicle containers.

**5. RQ<sub>5</sub>, The EDT physical object design, and (VCPD) mechanism**

The permutational vehicle containers drawers help reduce workers' fatigue at loading and unloading transportation activities (West TD, 2017). The design of drawers' capacity according to average orders and demands for a specific firm, while and motion mechanism is the same. The virtual and real design has been developed via the EDT framework and tried at a famous Egyptian company. Figure-6 shows the pattern of drawers, and the dimension is an inherent right to every company's needs according to the following calculations discussed in section 5.1.1. This idea is inspired by the supermarket tool at VSM design that regulates the customer demand leveling during transportation stages. The DT was run on a Laptop with an Intel i5 processor with 8 GB of RAM. The real-world scenarios aggregated as shown in Table-4 to be tested to measure the efficiency of the twin's model to avoid the economic parameters and develop the CAD model (Shao G., 2018). (figure 6)

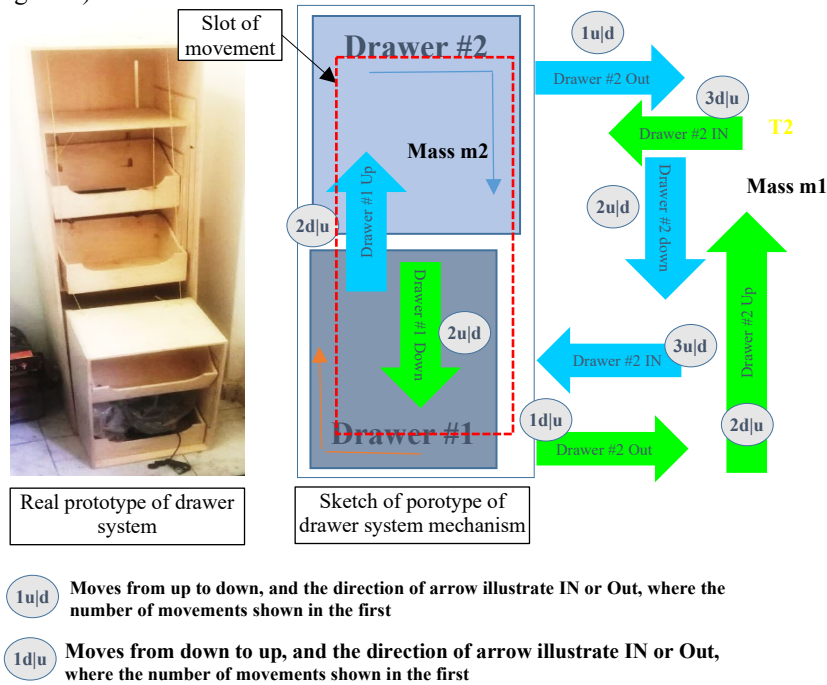


Figure 6. The proposed ergonomic vehicle's container drawers design

**5.1. The digital model of the physical object**

There is two-step of building the object's twin; the first is the economic drawer size according to use case, while the second calculates the suitable rope capable of loads movements up and down. The studied company (use case) will make its drawer!

**5.1.1. The first step**, the economic volumetric of the drawer, depends on the most loaded items of every company. The proposed model in RQ<sub>5</sub> considered a developmental model of Suzane Pedruzzi et al., 2016 and Lenz,O.U, 2020, via modifying some of the sets, parameters, and decision variables as follow in Table 3.

Table 3. Parameters, and decision variables

<b>Sets:</b>	
P	: Set of packed items $\delta_i$ , ranging from 1 to n, which $n \leq Permissible\ weight\ limit = \sum_{i=1}^P \lambda_i$
D	: Set of drawers $d_j$ , ranging from 1 to m, which have a different volumetric capacity
C	: Clusters of Near similarity $\delta_i$
<b>Parameters:</b>	



$n$	: # of items to be transported, which is in the bypass or backtrack direction of the vehicle.
$m$	: # of available drawers $d_j$ .
$G$	: A big number is used to balance the model logicity.
$g$	: A small number used to balance the model logicity
$V_r$	: Volumetric occupied in a real system
$V_m$	: Volumetric output of the model implementation
$\nabla_{aa}$	: Available stowed area at creating twin, can assume as a percentage values among 0:1, where 0% stipulate not available space to stow or (i.e., the drawer is full) and grows this value gradually to 1 that guarantee 100% (i.e., the drawer is empty).
$l_s$	: The loading sequence of $\delta_i$ , where the item with the highest value (area of upper face, weight) stowed first, before lowest, i.e., $\delta_{i-bottom}$ have surface face area $> \delta_{i-above}$
$sa_i (cm^3)$	: surface area of $\delta_{sa_{i-b}} > \delta_{sa_{i-a}}$ , where $\delta_{sa_{i-b}}$ refers to the surface area of item $i$ in layer 0 or below, while $\delta_{sa_{i-a}}$ refers to the surface area of item $i$ in layer 1 or above
$\lambda_i (kg)$	: The weights of items $\delta_i$ .
$l_a$	: The layer of stowage, ranging from 1: $la$ , where $la$ is a layer of the durability of $\delta_{sa_{i-b}}$ at the bottom
$du_i$	: The durability of $\delta_i$ to firmness another item above
$l_i, w_i, h_i$	: The length, width, and height of $\delta_i$
$L_j, W_j, H_j$	: The length, width, and height of $d_j$
$\varphi_i = \beta_j / \gamma_j$	: The covering of each $m^3$ of drawer's $d_j$ , i.e., the covering percentage of the total volume of the $d_j$ for the most famous $\delta_i$ loaded, while $\gamma_j$ is the volumetric capacity of the $d_j$ .
$\omega$	: Weight factor of the second parcel of a model, were ranging from 0.001 : 0.005
<b>The decision variables:</b>	
$x_i, y_i, z_i$	: Coordinates of lower left back corner of $\delta_i$
$l'_{xi}, l'_{yi}, h'_{zi}$	: Check if the length of $\delta_i$ is parallel to the X, Y, or Z-axis, $l'_{xi} = 1$ if the length of $\delta_i$ Parallel to the x-axis, while set 0 otherwise, also for other lengths.
$w'_{xi}, w'_{yi}, w'_{zi}$	: Check if the width of $\delta_i$ is parallel to the X, Y, or Z-axis, $w'_{xi} = 1$ if the width of $\delta_i$ Parallel to the y-axis, while set 0 otherwise, also for other lengths.
$h'_{xi}, h'_{yi}, h'_{zi}$	: Check if the width of $\delta_i$ is parallel to the X, Y, or Z-axis, $h'_{xi} = 1$ if the height of $\delta_i$ Parallel to the z-axis, while set 0 otherwise, also for other lengths.
$a_{ij}$	: Assignment of $\delta_i$ to $d_j$ , where if $a_{ij} = 1$ refers to placing this item in drawer j, and set by 0 otherwise.
$d'_j$	: Check if $d_j$ is used or not, where if $d_j = 1$ means it used and 0 otherwise.
$a'\Psi_{ikj}$	: Check if $\delta_i$ and $\delta_k$ are placed in the $d_j$ , where $a'\Psi_{ikj} = 0$ is assigned to $d_j$ , while 1 otherwise.
$l_{ik}, r_{ik}, bh_{ik}, ah_{ik}, bl_{ik}, ab_{ik}$	: Where relative position between two items, i.e., the variable $l_{ik} = 1$ if the $\delta_i$ is to left of $\delta_k$ , with taking into account $i \neq k$ , as same, other variables refer to $\delta_i$ is to right, behind, ahead, below, or above $\delta_k$ .

The digital twin of 'VCPD' is clarified in integrated three parcels identify the trial of optimizing the transportation capacity, as shown in Eq. (1), as discussed by (Siboni. S., 2020 and Piotr Pięta, 2021), which tailor the drawer dimensions according to the best fit of specific items.

$$V_m = \sum_{j \in D} \varphi_i (L_j, W_j, H_j n_j - \sum_{i \in P} l_i, w_i, h_i a_{ij}) + \omega (\sum_{i \in P} z_i + \sum_{i \in P} x_i + \sum_{i \in P} y_i) - \sum_{\delta_i=1}^P \lambda_i \dots (1)$$

Although, the  $d_j$ , dimension based on clustering the common stowage items (i.e., high demanded items) and studied into foursquare clusters side lengths of and cover the whole mesh of drawer with bins, counting the containers covering the area with ( $\varphi$ ). As the size of each cluster varies, the total number of clusters changes as well; the theoretical drawer capacity is the ratio of covering logs ( $\varphi$ ) divided by  $\log(1/\delta)$  when  $\delta$  is trending to 0, as illustrated in Eq. (2).

$$\varphi_i = \lim_{\delta \rightarrow 0} \frac{\log(\varphi)}{\log(\frac{1}{\delta})} \dots (2)$$

In most cases, however, it is not possible to  $\delta$  take the value of 0 directly. Furthermore, while altering the  $\delta_{xi}$  of items, the proportion of  $\log_2(\varphi)$  to  $\log_2(\frac{1}{\delta})$  does not take on a fixed value but instead stays within a steady ent'actes, which

are precisely described via the above parameters. Such, counting the changeable number ( $\varphi$ ) of identical objects with different side lengths  $l_i$  repeatedly and sketch versus ( $\varphi$ ) on a log-log plot scale as shown in Figure-7, gives a linear relation using the least square method, while the utter value of its decline is the recommended  $d_j$  size, which declares the amount of the self-identical proportion in statistics. Using the least-squares approach and a linear equation, the  $d_j$  dimension is calculated according to the next precautions representative in Eqn. from (3) to (20) as deduced from (Luzie Helfmann, 2021). The number of  $d_j$  can be computed by Eq. (3)

$$D_j = \frac{n \sum_{i=1}^n x_i y_i - \sum_{i=1}^n x_i \sum_{i=1}^n y_i}{n \sum_{i=1}^n x_i^2 - (\sum_{i=1}^n x_i)^2} \dots (3)$$

Whether the eqn. (4 and 5) interest in checking if two items  $\delta_i$  and  $\delta_k$  are inside the same drawer, while Eqn. (6-11) forbids overlapping situations at any side, below, or above.

$$2 - a_{ij} - a_{kj} \geq ga' \Psi_{ikj} \quad \forall i, k \in P, j \in D \dots (4)$$

$$2 - a_{ij} - a_{kj} \geq Ga' \Psi_{ikj} \quad \forall i, k \in P, j \in D \dots (5)$$

$$x_i + l_i l_{x_i} + w_i (l_{z_i} - w_{y_i} + h_{z_i}) + h_i (1 - l_{x_i} - l_{z_i} + w_{y_i} - h_{z_i}) - a' \Psi_{ikj} G \leq x_k + (1 - l_{ik}) G \quad \forall i, k \in P: i \neq k \dots (6)$$

$$x_k + l_k l_{x_k} + w_k (l_{z_k} - w_{y_k} + h_{z_k}) + h_k (1 - l_{x_k} - l_{z_k} + w_{y_k} - h_{z_k}) - a' \Psi_{ikj} G \leq x_i + (1 - r_{ik}) G \quad \forall i, k \in P: i \neq k \dots (7)$$

$$y_i + w_i w_{y_i} + l_i (1 - l_{x_i} - l_{z_i}) + h_i (l_{x_i} + l_{z_i} - w_{y_i}) - a' \Psi_{ikj} G \leq y_k + (1 - bh_{ik}) G \quad \forall i, k \in P: i \neq k \dots (8)$$

$$y_k + w_k w_{y_k} + l_k (1 - l_{x_k} - l_{z_k}) + h_k (l_{x_k} + l_{z_k} - w_{y_k}) - a' \Psi_{ikj} G \leq y_i + (1 - ah_{ik}) G \quad \forall i, k \in P: i \neq k \dots (9)$$

$$z_i + h_i h_{z_i} + w_i (1 - l_{z_i} - h_{z_i}) + l_i l_{z_i} - a' \Psi_{ikj} G \leq z_k + (1 - bl_{ik}) G \quad \forall i, k \in P: i \neq k \dots (10)$$

$$z_k + h_k h_{y_k} + w_k (1 - l_{z_k} - h_{z_k}) + l_k (l_{z_k}) - a' \Psi_{ikj} G \leq z_i + (1 - ab_{ik}) G \quad \forall i, k \in P: i \neq k \dots (11)$$

While designing the drawer  $d_j$ , face the feasibility of storage area are available or not to most demanded items (Kong, L., 2020). Therefore, the next eqn. (12-15) Guarantee the support area's existence so that the things are supported over each other safely. Variable  $bl_{ik}$  is equal to 1 when  $\delta_i$  is below  $\delta_k$  and then precautions (12) to (15) are activated.

$$x_i + l_i l_{x_i} + w_i (1 - l_{x_i}) + (1 - bl_{ik}) G \geq x_k \quad \forall i, k \in P: i \neq k \dots (12)$$

$$y_i + l_i l_{y_i} + w_i (1 - l_{y_i}) + (1 - bl_{ik}) G \geq y_k \quad \forall i, k \in P: i \neq k \dots (13)$$

$$x_i + l_i l_{x_i} + w_i (1 - l_{x_i}) - x_k + (1 - bl_{ik}) G \geq (l_k l_{x_k} + w_k (1 - l_{x_k})) \quad \forall i, k \in P: i \neq k \dots (14)$$

$$y_i + l_i l_{y_i} + w_i (1 - l_{y_i}) - y_k + (1 - bl_{ik}) G \geq (l_k l_{y_k} + w_k (1 - l_{y_k})) \quad \forall i, k \in P: i \neq k \dots (15)$$

When the items  $\delta_i$  and  $\delta_k$  in the same  $d_j$ , then must check the relative positioning between them via precaution shown in Eq. (16)

$$l_{ik}, r_{ik}, bh_{ik}, ah_{ik}, bl_{ik}, ab_{ik} \geq 1 - a' \Psi_{ikj} \dots i, k \in P: i \neq k; j \in D \dots (16)$$

But, what about if the  $\delta_i$  assigned to two different  $d_j$ . Therefore, the Eqn. (17, 18) formulated to prevent that.

$$\sum_{j \in D} a_{ij} = 1, \quad \forall i \in P \dots (17),$$

$$\sum_{i \in P} a_{ij} \leq Gn_j, \quad \forall j \in D \dots (18)$$

At this stage, design the drawers  $d_j$  according to most demanded items  $\delta_i$  and placed in a specific drawer, but must check from its fitting in this place by reducing the generated data (Iaroslav., 2021). Therefore, the Eqn. (19-22) interest

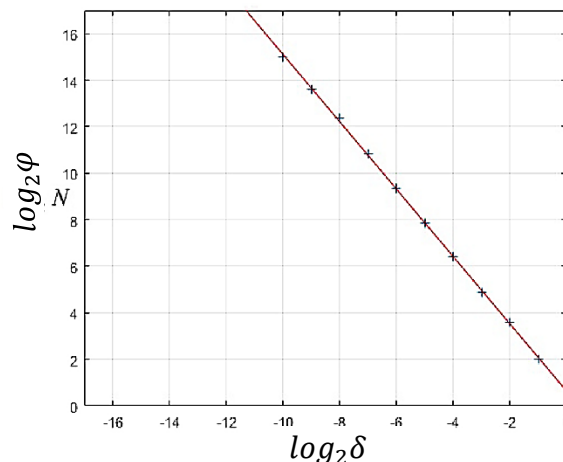


Figure 7. The linear fit ramp with LSM, through eleven variant points of different  $\varphi$  and  $\delta$  are chosen for the studying use case company.

(Figure 7) in minimizing the wasted area in the physical dimensions of the drawer  $d_j$ , and ensure that the dimensions of every item  $\delta_i(l_{xi}, w_{xi}, \text{ and } h_{xi})$  must be parallel to one side of the drawer  $d_j$

$$x_i + l_i l_{xi} + w_i(l_{zi} - w_{yi} + h_{zi}) + h_i(1 - l_{xi} - l_{zi} + w_{yi} - h_{zi}) \leq L_j + (1 - a_{ij})G \quad \forall i \in P, j \in D, \text{ and } l_{xi} + l_{yi} + l_{zi} = 1 \dots (19)$$

$$y_i + w_i w_{yi} + l_i(1 - l_{xi} - l_{zi}) + h_i(l_{xi} + l_{zi} - w_{yi}) \leq W_j + (1 - a_{ij})G \quad \forall i \in P, j \in D \text{ and } w_{xi} + w_{yi} + w_{zi} = 1 \dots (20)$$

$$z_i + h_i h_{yi} + w_i(1 - l_{zi} - h_{zi}) + l_i l_{zi} \leq H_j + (1 - a_{ij})G \quad \forall i \in P, j \in D \text{ and } h_{xi} + h_{yi} + h_{zi} = 1 \dots (21)$$

$$l_{xi} + w_{xi} + h_{zi} \text{ and } l_{yi} + w_{yi} + h_{yi} \text{ and } l_{zi} + w_{zi} + h_{zi} = 1 \quad \forall i \in P \dots (22)$$

The previous precautions of the proposed design guarantee placing all  $\delta_i$  in specific  $d_j$  and parallel to its side to assigned drawer at a specific position, with restricted reciprocal these items. Therefore, Eq. (23) allows reciprocal positions to meet the best fit and achieve maximum utilization via checking where:

$$l_{ik} = r_{ik}, bh_{ik} = ah_{ik}, bl_{ik} = ab_{ik} \quad \forall i, k \in P: i \neq k \dots (23)$$

The last precaution is to respect the durability  $du_i$  of items  $\delta_i$  in  $l_{a1}$  to be more than in  $l_{a2}$ , and respect also the surface of the upper face as formulated in Eq. (24)

$$\sum_{i=1 \in l_{a1}}^n sa \times du_i / \lambda_i \geq \sum_{i=1 \in l_{a2}}^n sa \times du_i / \lambda_i \quad \forall i \in d_j \dots (24)$$

When implementing this model for specific clustered items can activate all precautions from (4) to (24) help in discovering the dimension of every drawer  $d_j$  and get  $l_i = 105 \text{ cm}, w_i = 0.92 \text{ m}, \text{ and } h_i = 0.62 \text{ cm}$ . Therefore,  $d_j = 0.6m^3$  of different items respect Eq. (24) as a safe condition to transport the items safely. The box may have a square/rectangular base and a mesh bottom. Material costs of drawer  $d_j = \$5.85$  per  $m^2$ . The following section helps in deciding the most economical transportation capacity.

Table 4. Information from real-world scenarios

cluster	Demanded items							drawer V: Volume $D_j m^3$	Calculations					1 trip		Increased trips due to enhancing
	No. of trips/year	N: No. of orders in each cluster	Similar durability in a cluster	similar surface face in a cluster	Items dimensions $m$				No. of items picking < N	V <sub>m</sub> : Volumetric capacity $m^3$	Not occupied spaces	Percentage of occupation	Cost losses of unused area \$	Trip time enhancement		
					$l_{xi}$	$w_{xi}$	$h_{xi}$									
1	35	25	yes	no	0.1	0.6	0.3	0.5	20	0.36	0.14	72.0%	0.8	30.0%	11	
		12	no	no	0.2	0.3	0.13	0.8	10	0.078	0.722	9.7%	4.2	4.1%	1	
		32	no	yes	0.18	0.23	0.35	0.5	30	0.435	0.066	86.9%	0.4	36.2%	13	
2	12	20	yes	yes	0.15	0.31	0.13	0.5	20	0.121	0.379	24.2%	2.2	10.1%	1	
		20	yes	yes	0.18	0.23	0.23	0.5	20	0.391	0.31	38.1%	1.8	15.9%	2	
		25	no	no	0.18	0.23	0.35	0.8	20	0.290	0.511	36.2%	3	15.1%	2	
3	20	8	yes	yes	0.1	0.3	0.3	0.5	8	0.072	0.428	14.4%	2.5	6.0%	1	
		33	no	no	0.2	0.3	0.3	0.85	30	0.44	0.31	63.5%	-1.1	-ve	0	
		20	yes	yes	0.1	0.3	0.3	0.5	20	0.18	0.32	36.0%	1.9	15.0%	3	
4	20	12	no	yes	0.15	0.3	0.35	0.40	10	0.158	0.243	39.4%	1.4	16.4%	3	
		10	yes	yes	0.1	0.3	0.3	0.5	10	0.090	0.41	18.0%	2.4	7.5%	2	
		34	no	yes	0.17	0.32	0.34	0.40	30	0.555	Full	-----	-0.9	-ve	0	
5	25	19	no	yes	0.1	0.3	0.3	0.40	15	0.335	0.265	33.8%	1.6	14.1%	4	
		19	no	no	0.25	0.45	0.32	0.8	18	0.348	0.152	81.0%	0.9	33.8%	8	
		46	no	yes	0.15	0.3	0.38	0.8	40	0.684	0.116	85.5%	0.7	35.6%	9	
6	17	10	yes	yes	0.18	0.3	0.38	0.5	10	0.205	0.295	41.0%	1.7	17.1%	3	
		21	no	no	0.18	0.33	0.35	0.85	20	0.216	0.034	92.4%	0.2	38.5%	7	
7	12	21	yes	no	0.19	0.36	0.28	0.40	20	0.383	0.017	95.8%	0.1	39.9%	5	
		38	no	yes	0.12	0.3	0.23	0.40	30	0.348	0.152	62.1%	0.9	25.9%	3	
8	35	59	no	yes	0.1	0.32	0.3	0.6	50	0.480	0.12	80.0%	0.7	33.3%	12	
		41	yes	no	0.1	0.32	0.3	0.6	40	0.384	0.216	64.0%	1.3	26.7%	9	
		33	no	yes	0.1	0.3	0.3	0.6	30	0.270	0.33	45.0%	1.9	18.8%	7	

Table-4 shows the number of clustered orders to be stowed in the designed drawer as discussed in Eq. (1) to Eq. (3) and respects all precautions Eqn. (4 to 24), all negative values in occupation capacity replaced to full or loss 0%, and the reduction of costs approaching 8841 \$. The model presented a bad drawer design if the  $\delta_i$  have different durability and upper face; otherwise, the model presents a volumetric with the minimum waste unused area. The enhancement appeared in the last column compensates by increasing the number of trips and the transported items. The Estimated annual gains (\$)  $\cong$  928346 as shown in Table-5.

**5.1.1.1. Draw a sketch RQs!**

The particular case is to design the base as square, so we will just use ' $L_p$ ' for both lengths, the drawer has 4 sides with height  $h_h$ , and square mesh bottom. The drawer shape could be designed out like Figure-6, where Volume =  $L_j \times L_j \times h_j = L_j^2 h_j$ , and we are told that the volume should be  $0.5m^3$ :  $L_j^2 h_j = 0.5$ . The total area of all sides =  $4 \times L_j \times h_j = 4L_j h_j$ , while the Total Area  $4 \times L_j^2$ , then the Total material sides used =  $4 \times L_j \times h_j + 4 \times L_j^2$ .

**5.1.1.2. Make a Single Formula for Cost**

We want a single formula for cost =  $\$5.85 \times$  Area of drawer =  $\$5.85 \times (4 \times L_j \times h_j + 4 \times L_j^2)$ . And that is the cost when we know  $L_j$ , and  $h_j$ . Therefore, the Cost =  $\$5.85 \times (4 \times L_j \times 0.6/L_j^2 + 4L_j^2)$  ... (25), and computed to Cost be =  $\$5.85 \times (2/L_j + 4L_j^2)$ .

Table 5. Financial gains for the company when implementing the permutational drawers (VCPD )

Situation	Trips capacities $m^3/year$	Trip Cost \$ per / transported $m^3$	No. of Trips		Total Trips' profit		Financial gains		
			Company	EDT	Company	EDT	ROI \$	%	
	1245.5								
Before	2235.2	13075.92	176	-----	2301362 \$	-----	-----	-----	
After	2756.8	21917.03	-----	295		1373016.6 \$	928346	59	
			Reduction in \$ = 8841.1 \$				-----	-----	
			Estimated annual gains (\$) $\cong$ 928346						

**5.1.2. The second step:** The drawers move up and down through the slots' stream and are controlled by ropes/chains that slide over horizontal pulleys; as shown in Figure-8 (Cooper, C., 2020a ), every drawer has mass  $m_1$ , and another reciprocity moves in vice direction is  $m_2$ . The design has two sides, the drawers' dimension, and the rope capability. Therefore, Eq. (26) and Eq. (27) discuss a simple EDT model that achieves the requirement.  $T - m_1 \times g = m_1 \times a$  ... (26), while  $m_2 \times g - T = m_2 \times a$  ... (27). When sum the two equations can expect with rope material used in a specific use case.  $m_2 \times g - m_1 \times g = (m_2 - m_1) \times a$ , then the acceleration of falling the full occupied is calculated the Eq. (28)  $a = \frac{(m_2 - m_1) \times g}{m_2 + m_1}$  ... (28). Therefore, the tension required for completing the sliding motion is deduced from Eq. (29)  $T = m_1 \times g + m_2 \times g$  ... (29). For example, if  $m_1= 50$  kg (full drawer) and  $m_2=5$ kg (when empty), there is a need to move up and pull the full one down. The acceleration, in this case, is  $8.035 m/s^2$ . While the tension required is 892.8 N. The design enhanced to achieve companies' requirements and reduce workers' fatigue 8.

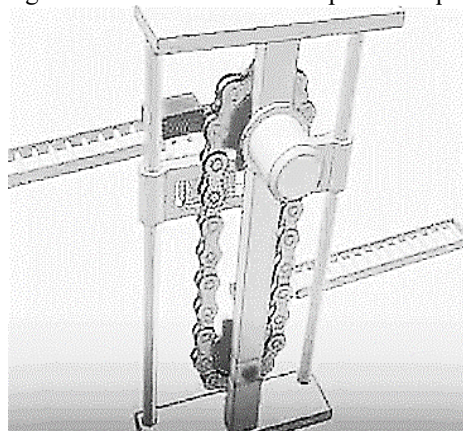


Figure 8. The rope mechanism

## 6. Conclusion

The digital twins are a future of development and control for transportation schemes to acquire adaptation skills (flexibility) to keep up with the VOC (i.e., the voice of customer) of satisfaction factors, whether the products or services are delivered in minimum time through distribution activities. The DT receives the VOC and/or stakeholders data fed to the IoT dataset to create a perception of steps to enhance and develop the designed product in its first generation schemes, discussed in Eqn. (1-24). Some of the indicators, such as the over-processing (waste) activities reduced by 27%, the average execution time of loading and unloading activities reduced by 40%, and the delivery time by 15%. The future of transportation lies in employing digital twins to increase serviceability for related KPI and cut expenses, which will become increasingly popular. By 2025, Up to 89% of all services must have their DT models controlled via IoT platforms in real-time. Nearly 36% of executives across various industries are aware of the benefits of digital twinning, with almost half aiming to implement it by 2028 (ASME, 2021). As time goes on, digital twin technology establishes itself as one of the essential software tools for changing product creation. The DT models are designed to study how to reduce the efforts, service time, service costs and increase the performance up to 59%, as shown in Table-5 (i.e., this value is different according to the studied case). Also, test, experiment, and develop the mechanism of the physical object to achieve the previous aims. The proposed EDT is ready to assume any inputs according to the use case to establish the presented object.

**Acknowledgments:** Special thanks to the participants in the Scientific Day Team of the Department of Industrial Engineering workshop discussed and to the expert reviewers of the template. Thanks to the Design Society for supporting the special interest group at Zagazig University USCC.

## Reference

- ASME, 7 Digital Twin Applications for Transportation, Mar 17, (2021). Mark Crawford is technology writer based in Corrales, N.M. <https://www.asme.org/topics-resources/content/7-digital-twin-applications-for-transportation>
- Ahmed M. Abed. Adjust Jidoka Occupational Fatigue to Reduce Idle times using Data Mining as Lean Tool', EIJEST, The Egyptian International Journal of Engineering Science and Technology, Vol. 19, No. 2, Pp. 312-318, 2016. [https://eijest.journals.ekb.eg/article\\_97147.html](https://eijest.journals.ekb.eg/article_97147.html)
- Ahmed M. Abed, Samia Elattar, Tamer Gaafar, Fadwa Alrowais, " The Neural Network revamping the process's reliability in deep Lean via internet of things", Processes (ISSN 2227-9717), *Processes* 2020, vol. 8, no. 6, pp. 729, 2020; <https://www.mdpi.com/2227-9717/8/6/729>
- Ahmed M. Abed, Samia Elattar, Tamer Gaafar, Fadwa Alrowais, Artificial Poka-Yoke Increases Process Reliability via a Hybrid of the Neural Network with ARIMA Results, [International Journal of Mechanical and Outputs Engineering Research and Development](http://www.tjprc.org/view_paper.php?id=12579), 2020, Vol. 10–2, Issue date Apr-30 2020, pp. 931–954. IJMPERDAPR202092, DOI: 10.24247/ijmperdapr202092, ISSN(P): 2249–6890; ISSN(E): 2249–8001 [http://www.tjprc.org/view\\_paper.php?id=12579](http://www.tjprc.org/view_paper.php?id=12579)
- Ahmed M. Abed, Tamer S. Gaafar, Reinforcing the Internet of things by Neural Network to enhance the processes' reliability via Poka-Yoke wirelessly to combat Covid19. International Conference on Industrial Engineering and Operations Management, Detroit, Michigan, USA, Aug. 10-14, 2020, 5th NA IEOM Society International pp. 2436-2449, ISSN: 2169-8767 ISBN: 978-0-9855497-8-7 <http://www.ieomsociety.org/detroit2020/papers/76.pdf>
- Ahmed M. Abed, Samia Elattar, Tamer Gaafar, Fadwa Alrowais, (2020). Artificial Poka-Yoke Increases Process Reliability Via A Hybrid Of The Neural Network With ARIMA Results, International Journal of Mechanical and Production Engineering Research and Development, 2020, Vol. 10–2, Issue date Apr-30 2020, pp. 931–954. IJMPERDAPR202092, DOI : 10.24247/ijmperdapr202092, ISSN(P): 2249–6890; ISSN(E): 2249–8001 [http://www.tjprc.org/view\\_paper.php?id=12579](http://www.tjprc.org/view_paper.php?id=12579)
- Ahuett-Garza H and Kurfess T.',A brief discussion on the trends of habilitating technologies for industry 4.0 and smart transportation'. *Transportation Letters* 15 pp. 60–63, 2018.
- Alberto Merced Castro Valencia., Monetary Policy between Mexico, United States of America, and Canada, South Florida Journal of Development, Miami, Vol. 3 No. 1 , pp. 137-145, 2022. DOI: <https://doi.org/10.46932/sfjdv3n1-010>
- Berti, J.G. and Deluca, LS, International Business Machines Corp. Digital agreement management on digital twin ownership change. US Patent Application vol. 16, pp. 392-426, 2019.

- Bolton D. What Are Digital Twins and Why Will They Be Integral to The Internet of Things?, Connected World, November 2, 2016.
- Bao, J., Guo, D., Li, J. and Zhang, J., 'The modelling and operations for the digital twin in the context of manufacturing. Enterprise Information Systems', 13(4), pp.534-556, 2019.
- Boschert S, Rosen R., Digital Twin - The Simulation Aspect In: Hehenberger P, Bradley D, editors. Mechatronic Futures. Cham: Springer International Publishing, 2016.
- Coronado PDU, Lynn R, Louhichi W, Parto M, Wescoat E, and Kurfess T., Part data integration in the shop floor digital twin: mobile and cloud technologies to enable a transportation execution system. Journal of Transportation Systems 48, pp. 25–33, 2019.
- Cooper, C., Wang, P., Zhang, J., Gao, R.X., Roney, T., Ragai, I. and Shaffer, D. Convolutional neural network-based tool condition monitoring in vertical milling operations using acoustic signals, Procedia Manufacturing 49: pp. 105–111, 2020a.
- DUBLIN, March 24, 2020 /PRNewswire/ -- The "[Digital Twins Market by Technology, Solution, Application, and Industry Vertical 2020-2025](#)" report has been added to ResearchAndMarkets.com's offering.
- Eckhart, M. and Ekelhart, A., 'January., A specification-based state replication approach for digital twins'. In Proceedings of the 2018 Workshop on Cyber-Physical Systems Security and Privacy, pp. 36-47, 2018.
- Grieves M. (2005). Product lifecycle management: driving the next generation of lean thinking: driving the next generation of lean thinking: driving the next generation of lean thinking. McGraw Hill Professional; 2005 Oct 26.
- Grieves, M.' Digital twin: transportation excellence through virtual factory replication'. White paper, 1, pp.1-7, 2014.
- Grieves, M. and Vickers, J., Digital twin: Mitigating unpredictable, undesirable emergent behavior in complex systems'. In Transdisciplinary perspectives on complex systems (pp. 85-113). 2017, Springer, Cham.
- Gartner. 'Gartner Survey Reveals Digital Twins Are Entering Mainstream Use'. 2019, <https://www.gartner.com/en/newsroom/press-releases/2019-02-20-gartner-survey-reveals-digital-twins-are-entering-mainstream-use>
- GE. 2018. What is Digital Twin? <https://www.ge.com/digital/applications/digital-twin>
- Guodong Shao and Moneer Helu. 'Framework for a digital twin in manufacturing: scope and requirements', Engineering Laboratory, National Institute of Standards and Technology., 2020,100 Bureau Drive, Stop 8260, Gaithersburg, MD 20899 USA. Version of Record: <https://www.sciencedirect.com/science/article/pii/S2213846319301312>
- Gottfried Hastermann, Maria Reinhardt, Rupert Klein and Sebastian Reich., Balanced data assimilation for highly oscillatory mechanical systems. Communications in Applied Mathematics and Computational Science. Vol. 16, No. 1, pp. 119–154, 2021. [10.2140/camcos.2021.16.119](https://doi.org/10.2140/camcos.2021.16.119)
- Haag, S., and Anderl, R., Digital Twin - Proof of concept. Transportation Letters 15 pp. 64–66, 2018
- Iaroslav I., Roman S., Roman J., and Petr L., An effective data reduction model for machine emergency state detection from big data tree topology structures, Vol. 31, no. 4, and pp. 601 – 611. 2021. <https://doi.org/10.34768/amcs-2021-0041>
- Islam, M., Inan, T., Rafi, S., Akter, S., Sarker, I.H. and Islam, A., A systematic review on the use of AI and ML for fighting the COVID-19 pandemic, IEEE Transactions on Artificial Intelligence vol. 3, pp. 258–270, 2020.
- Kong, L., Qu, W., Yu, J., Zuo, H., Chen, G., Xiong, F., Pan, S. and Siyu Lin, M.Q. Distributed feature selection for big data using fuzzy rough sets, IEEE Transactions on Fuzzy Systems vol. 28, no. 5, pp. 846–857, 2020.
- Lenz, O.U., Peralta, D., and Cornelis, C. Fuzzy-rough-learn 0.1: A Python library for machine learning with fuzzy rough sets, in R. Belloet al. (Eds), Rough Sets, Lecture Notes in Computer Science, Vol. 121 no. 79, Springer, Cham, pp. 491–499, 2020.
- Luzie, H., Nataša D. C., and Ana D., Stefanie Winkelmann and Christof Schütte., From interacting agents to density-based modeling with stochastic PDEs. Communications in Applied Mathematics and Computational Science. Vol. 16, no. 1, pp. 1–32, 2021.
- Piotr, P., and Tomasz S., Applications of rough sets in big data analysis: An overview, [Vol.31, no. 4](#), pp. 659 – 683, 2021. <https://doi.org/10.34768/amcs-2021-0046>
- Roberto Pñuyo Muñoz, Magister Rosmel Iván Rodríguez Peceros, Magister Elizabeth Urrutia Huamán, Maribel Osís Huamán. Application of inferential reading comprehension for the achievement of mathematical problem solving skills using Pólya's method in EPIME-UNTELS students., South Florida Journal of Development, Miami, Vol. 3 No. 1, pp. 894-905., DOI: 10.46932/sfjdv3n1-068

- Siemens. 2018. Digital Twin, <https://www.plm.automation.siemens.com/global/en/our-story/glossary/digital-twin/24465>
- Shao G and Kibira D. (2018). Digital Transportation: Requirements and Challenges for Implementing Digital Surrogates." Proceedings of the 2018 Winter Simulation Conference, edited by Rabe M, et al. 1226–1237. Piscataway, New Jersey: Institute of Electrical and Electronics Engineers, Inc.
- Siboni, S. and Cohen, A. Anomaly detection for individual sequences with applications in identifying malicious tools, Entropy, vol. 22, no. 6: 649, (2020).
- Schleich, B., Anwer, N., Mathieu, L. and Wartzack, S. Shaping the digital twin for design and outputs engineering. CIRP Annals, vol. 66, no. 1, pp.141-144, 2017.
- Suzane, P., Luiz, P., Rodrigo de A., and Bianca P., A mathematical model to optimize the volumetric capacity of trucks utilized in the transport of food products. Gest. Prod., São Carlos, vol. 23, no. 2, p. 350-364, 2016. <http://dx.doi.org/10.1590/0104-530X1898-14>
- Talkhestani, B.A., Jazdi, N., Schlögl, W. and Weyrich, M., Consistency check to synchronize the Digital Twin of transportation automation based on anchor points. Procedia Cirp', vol. 72, pp.159-164, 2018.
- Talkhestani, B.A., Jung, T., Lindemann, B., Sahlab, N., Jazdi, N., Schloegl, W. and Weyrich, M. An architecture of an intelligent digital twin in a cyber-physical production system. Automatisierungstechnik, vol. 67, no. 9, pp.762-782, 2019.
- West, TD. and Blackburn, M., Is Digital Thread/Digital Twin Affordable? A Systemic Assessment of the Cost of DoD's Latest Manhattan Project. Procedia computer science, 114, 2017, pp.47–56, 2017.
- Zipper, H. and Diedrich, C., September. Synchronization of industrial plant and digital twin. In 2019 24<sup>th</sup> IEEE international conference on emerging technologies and factory automation (ETFA), pp. 1678-1681, 2019.