## Development of Electric Vehicle Simulation Model with DC BUS V/I-dependent Efficiency Map for Si IGBT and SiC MOSFET-based Traction Inverters

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## Abstract

In the realm of electrified vehicle development, vehicle simulations employing drive cycle inputs typically span thousands of seconds. Within this time domain, executing inverter motor control simulations with step sizes smaller than 1ms is not practical. To address this challenge, this research proposes a method of modeling electrified vehicles using an inverter efficiency map predicated on DC bus voltage and current. Theoretical analyses have corroborated that pivotal factors—such as collector voltage and current for Insulated-Gate Bipolar Transistors (IGBT) and Metal-Oxide-Semiconductor Field-Effect Transistors (MOSFET) —are dictated by the DC bus voltage and current, provided that the switching frequency and modulation index are fixed. Hence, power electronics simulations of inverters can be conducted at varying DC bus voltages and currents to create efficiency maps for prospective semiconductors. Tests have been performed on the Silicon IGBT IKW50N60DTP and Silicon Carbide MOSFET C3M0015065K. With the inclusion of the developed efficiency maps, a Tesla Model S vehicle model has been constructed and simulated. The simulation results from the combined Urban Dynamometer Driving Schedule (UDDS) and Highway Fuel Economy Test (HFET) drive cycle confirm that the SiC MOSFET-based inverter boasts greater and more consistent efficiency than its Si IGBT counterpart.

## Keywords

Electric vehicle, Simulation, Inverter, SiC MOSFET, IGBT.

## **1. Introduction**

Simulation based on test data is frequently employed for tasks such as component sizing, range prediction, and other performance estimations in the development of electrified vehicles (Powell et al. 1998). However, when it comes to evaluating a candidate system for which some test data—such as efficiency—is unavailable, executing an accurate simulation can be challenging.

Traction inverters serve as a prime example of these challenges. The switching frequency of inverter semiconductors is at the kHz level, necessitating a simulation step size of less than 1ms. However, performing simulations at this level of granularity for vehicle-level applications is not feasible, considering that a drive cycle can span thousands of seconds. Thus, there is a clear need for more adaptable and scalable simulation methods in the field of electrified vehicle development. In a previous study, Zhu et al. (2018) introduced a method that interpolates vehicle operating conditions at the inverter's switching period resolution. However, this approach necessitates repetitive work across various drive cycles, and experimental testing is still indispensable. In another study, a component loss map was generated from test data and integrated into the vehicle model to calculate efficiency (Su et al. 2019). While this method provides useful insights, it requires the acquisition of substantial test data, which can prove challenging when assessing multiple candidate semiconductor devices. Therefore, both approaches underscore the need for efficient methodologies that can navigate these complexities in the field of electrified vehicle development.

In this paper, we propose a method to estimate the power loss of a traction inverter using DC bus voltage and current. Based on our proof that the power loss of a traction inverter is determined by the DC bus voltage and current, we conduct a component-level simulation to estimate power loss at each operating point. This simulation can be performed in software such as PSpice, which utilizes a real component library, ensuring high accuracy in our results.

#### **1.1 IGBT Power Loss**

Miao et al. (2018) postulate that IGBT conduction loss can be represented as

$$P_{cond_{IGBT}} = \frac{1}{2} \left( V_{CEO} \cdot \frac{I_{ac}}{\pi} + r_C \cdot \frac{I_{ac}^2}{4} \right) + m \cdot \cos \varphi \cdot \left( V_{CEO} \cdot \frac{I_{ac}}{8} + r_C \cdot \frac{I_{ac}^2}{3\pi} \right)$$
(1)

Where  $V_{CEO}$  represents the threshold voltage drop of the IGBT,  $r_C$  represents the conduction resistance of the IGBT, and  $\cos \varphi$  represents the power factor of the inverter with a phase shift angle of  $\varphi$  between output voltage and current. These contributors are treated as constants when the inverter remains at a single operating point. The three-phase SPWM modulation factor *m* is equivalent to

$$n = \frac{2\sqrt{6} \cdot V_{ac,rms}}{3 \cdot V_{dc}} \tag{2}$$

Where  $V_{ac,rms}$  is the RMS AC line output voltage and  $V_{ac}$  is the input DC voltage.  $V_{ac,rms}$  is typically a fixed value.  $I_{ac}$  in (1) represents the amplitude of AC current output. The RMS AC current output  $I_{ac,rms}$  is obtained from  $I_{ac}$  via

$$I_{ac,rms} = \frac{I_{ac}}{\sqrt{2}} \tag{3}$$

For simulation, lossless operation is initially assumed to obtain operating setpoint conditions, then the losses from the obtained operating conditions are computed. Given the lossless operation assumption, AC voltage and current can be related to DC voltage and current via

$$P = V_{dc} \cdot I_{dc} = \sqrt{3} \cdot V_{ac,rms} \cdot I_{ac,rms} \cdot \cos \varphi = \sqrt{3} \cdot V_{ac,rms} \cdot \frac{I_{ac}}{\sqrt{2}} \cdot \cos \varphi$$
(4)

 $I_{ac}$ , then, is equivalent to

$$I_{ac} = \frac{\sqrt{2} \cdot V_{dc} \cdot I_{dc}}{\sqrt{3} \cdot V_{ac} \, rms \cdot \cos \varphi} \tag{5}$$

Substituting (2) and (5) into (1),  $P_{cond_{IGBT}}$  can be represented as

$$P_{cond_{IGBT}} = \frac{1}{2} \left( V_{CEO} \cdot \frac{\frac{\sqrt{2} \cdot V_{dc} \cdot I_{dc}}{\sqrt{3} \cdot V_{ac,rms} \cdot \cos \varphi}}{\pi} + r_{c} \cdot \frac{\left(\frac{\sqrt{2} \cdot V_{dc} \cdot I_{dc}}{\sqrt{3} \cdot V_{ac,rms} \cdot \cos \varphi}\right)^{2}}{4} \right) + \frac{2\sqrt{6} \cdot V_{ac,rms}}{3 \cdot V_{dc}} \cdot \cos \varphi$$

$$\cdot \left( V_{CEO} \cdot \frac{\frac{\sqrt{2} \cdot V_{dc} \cdot I_{dc}}{\sqrt{3} \cdot V_{ac,rms} \cdot \cos \varphi}}{8} + r_{c} \cdot \frac{\left(\frac{\sqrt{2} \cdot V_{dc} \cdot I_{dc}}{\sqrt{3} \cdot V_{ac,rms} \cdot \cos \varphi}\right)^{2}}{3\pi} \right)$$

$$(6)$$

Which simplifies to

$$P_{cond_{IGBT}} = \frac{4\sqrt{6} \cdot I_{dc}^2 \cdot V_{dc} \cdot r_c}{27\pi \cdot V_{ac,rms} \cdot \cos\varphi} + \frac{I_{dc}^2 \cdot V_{dc}^2 \cdot r_c}{12 \cdot V_{ac,rms}^2 \cdot \cos^2\varphi} + \frac{I_{dc} \cdot V_{CEO}}{6} + \frac{\sqrt{6} \cdot I_{dc} \cdot V_{dc} \cdot V_{CEO}}{6\pi \cdot V_{ac,rms} \cdot \cos\varphi}$$
(7)

Switching loss in the IGBT occurs in the transient state between conduction and cutoff. Miao et al. (2018) state that IGBT switching loss can be represented as

$$P_{SW_{Tr}} = f_{SW} \left( E_{on} + E_{off} \right) \cdot \frac{V_{dc}}{V_N} \cdot \frac{I_{dc}}{I_N} \cdot \left[ 1 + k_{E_{Tr}} \left( 125 - T_{j_{Tr}} \right) \right]$$
(8)

Where  $f_{SW}$  is the switching frequency,  $E_{on}$  represents the losses of conduction under rated conditions of the IGBT, and  $E_{off}$  represents the losses of cutoff under rated conditions of the IGBT.  $V_N$  and  $I_N$  are the nominal input DC voltage and DC current to the IGBT under rated conditions.  $V_{dc}$  and  $I_{dc}$  are the "actual" input DC voltage and DC current to the IGBT, and  $T_{jTr}$  is the IGBT junction temperature at the selected operating point. The losses under rated conditions are temperature-compensated via an experimentally derived correction coefficient  $k_{ETr}$  to adjust to the selected inverter operating point.  $f_{SW}$ ,  $E_{on}$ ,  $E_{off}$ ,  $V_N$ ,  $I_N$ ,  $k_{ETr}$ , and  $T_{jTr}$  remain constant while the inverter is operated at a given operating condition. Therefore,  $P_{SWTr}$  is expressed as a function of  $I_{dc}$  and  $V_{dc}$ .

The total power loss of the IGBT is

$$P_{Tr} = P_{cond_{IGBT}} + P_{SW_{Tr}} \tag{9}$$

Substituting (7) and (8) into (9) yields

$$P_{Tr} = \frac{4\sqrt{6} \cdot I_{dc}^{2} \cdot V_{dc} \cdot r_{c}}{27\pi \cdot V_{ac,rms} \cdot \cos\varphi} + \frac{I_{dc}^{2} \cdot V_{dc}^{2} \cdot r_{c}}{12 \cdot V_{ac,rms}^{2} \cdot \cos^{2}\varphi} + \frac{I_{dc} \cdot V_{CEO}}{6} + \frac{\sqrt{6} \cdot I_{dc} \cdot V_{dc} \cdot V_{CEO}}{6\pi \cdot V_{ac,rms} \cdot \cos\varphi} + f_{SW}(E_{on} + E_{off}) \cdot \frac{V_{dc}}{V_{N}} \cdot \frac{I_{dc}}{I_{N}} \cdot [1 + k_{E_{Tr}}(125 - T_{j_{Tr}})]$$

$$(10)$$

This derivation demonstrates that, for any given operating point of the IGBT-based inverter,  $P_{Tr}$  is a function of  $I_{dc}$  and  $V_{dc}$  as all other terms are constant.

Miao et al. (2018) state that diode conduction loss can be represented as

$$P_{cond_D} = \frac{1}{2} \left( V_{TO} \cdot \frac{I_{ac}}{\pi} + r_T \cdot \frac{I_{ac}^2}{4} \right) + m \cdot \cos \varphi \cdot \left( V_{TO} \cdot \frac{I_{ac}}{8} + r_T \cdot \frac{I_{ac}^2}{3\pi} \right)$$
(11)

Where  $V_{TO}$  is the threshold voltage drop of the diode and  $r_T$  is the conduction resistance of the diode, both of which are constants for a given inverter operating setpoint. Substituting (2) and (5) into (11),  $P_{cond_D}$  can also be represented as

$$P_{cond_{D}} = \frac{1}{2} \left( V_{TO} \cdot \frac{\sqrt{2} \cdot V_{dc} \cdot I_{dc}}{\pi} + r_{T} \cdot \frac{\sqrt{2} \cdot V_{dc} \cdot I_{dc}}{4} \right) + \frac{2\sqrt{6} \cdot V_{ac,rms}}{3 \cdot V_{dc}} \cdot \cos \varphi + \frac{\sqrt{2} \cdot V_{dc} \cdot I_{dc}}{3 \cdot V_{dc}} + \frac{\sqrt{2} \cdot V_{dc} \cdot I_{dc}}{3 \cdot V_{dc}} \cdot \cos \varphi \right)$$

$$(12)$$

Which simplifies to

$$P_{cond_D} = \frac{4\sqrt{6} \cdot I_{dc}^2 \cdot V_{dc} \cdot r_T}{27\pi \cdot V_{ac,rms} \cdot \cos\varphi} + \frac{I_{dc}^2 \cdot V_{dc}^2 \cdot r_T}{12 \cdot V_{ac,rms}^2 \cdot \cos^2\varphi} + \frac{I_{dc} \cdot V_{TO}}{6} + \frac{\sqrt{6} \cdot I_{dc} \cdot V_{dc} \cdot V_{TO}}{6\pi \cdot V_{ac,rms} \cdot \cos\varphi}$$
(13)

Miao et al. (2018) state that diode switching loss, which occurs in the transient state between cutoff and conduction, can be represented as

$$P_{SW_D} = f_{SW} \cdot E_{rec} \cdot \frac{V_{dc}}{V_N} \cdot \frac{I_{dc}}{I_N} \cdot \left[1 + k_{E_D} \left(125 - T_{j_D}\right)\right]$$
(14)

Where  $E_{rec}$  represents the reverse-recovery ("switching") loss of the diode under the rated conditions and  $T_{j_D}$  represents the diode junction temperature. The losses under rated conditions are temperature-compensated via an experimentally derived correction coefficient  $k_{E_D}$  to adjust to the selected inverter operating point.  $f_{SW}$ ,  $E_{rec}$ ,  $V_N$ ,  $I_N$ ,  $k_{E_D}$ , and  $T_{j_D}$  remain constant while the inverter is operated at a given operating condition. Therefore,  $P_{SW_D}$  is expressed as a function of  $I_{dc}$  and  $V_{dc}$ .

The total diode power loss is

$$P_D = P_{cond_D} + P_{SW_D} \tag{15}$$

$$P_{D} = \frac{4\sqrt{6} \cdot I_{dc}^{2} \cdot V_{dc} \cdot r_{T}}{27\pi \cdot V_{ac,rms} \cdot \cos\varphi} + \frac{I_{dc}^{2} \cdot V_{dc}^{2} \cdot r_{T}}{12 \cdot V_{ac,rms}^{2} \cdot \cos^{2}\varphi} + \frac{I_{dc} \cdot V_{T0}}{6} + \frac{\sqrt{6} \cdot I_{dc} \cdot V_{dc} \cdot V_{T0}}{6\pi \cdot V_{ac,rms} \cdot \cos\varphi} + f_{SW} \cdot E_{rec} \cdot \frac{V_{dc}}{V_{N}}$$

$$\cdot \frac{I_{dc}}{I_{N}} \cdot [1 + k_{E_{D}} (125 - T_{j_{D}})]$$

$$(16)$$

This derivation demonstrates that, for any given operating point of the IGBT-based inverter,  $P_D$  is a function of  $I_{dc}$  and  $V_{dc}$  as all other terms are constant.

### **1.2 SiC MOSFET Power Loss**

Gurpinar and Ozpineci (2018) indicate that SiC MOSFET forward conduction loss can be represented as  $P_{cond_M} = P_{cond_+} + P_{cond_-} + P_{dt_1} + P_{dt_2} - P_{dt_{red}}$ (17)

Where  $P_{cond_+}$  is conduction loss in the positive state,  $P_{cond_-}$  is conduction loss in the negative state,  $P_{dt_1}$  is the dead-time conduction loss in the 0 to  $\varphi$  region,  $P_{dt_2}$  is the dead-time conduction loss in the  $\varphi$  to  $\pi$  region, and  $P_{dt_{red}}$  is the reduction in conduction loss due to dead-time duration reducing the total conduction time.  $P_{cond_+}$  and  $P_{cond_-}$  can be expressed as

$$P_{cond_{+}} + P_{cond_{-}} = \frac{r_{DS} \cdot I_{ac,rms}^{2}}{8}$$
(18)

Where  $r_{DS}$  is the on-state switch resistance.  $P_{dt_1}$  can be expressed as

$$P_{dt_1} = \frac{t_{dt} \cdot f_{SW}}{\pi} [V_{th} \cdot \frac{I_{ac}}{2} (1 - \cos(-\varphi)) + \frac{I_{ac}^2}{4} \cdot r_{SD} \left(\frac{\varphi}{2} - \frac{\sin(2\varphi)}{4}\right)]$$
(19)

Where  $t_{dt}$  is the dead-time duration,  $V_{th}$  is on-state threshold voltage of the body diode, and  $r_{SD}$  is on-state resistance of the body diode.  $P_{dt_2}$  can be expressed as

$$P_{dt_2} = \frac{t_{dt} \cdot f_{SW}}{\pi} [V_{th} \cdot \frac{I_{ac}}{2} \cdot (\cos(\pi - \varphi) - 1) + \frac{I_{ac}^2}{4} \cdot r_{SD} \cdot \left(\frac{\pi - \varphi}{2} + \frac{\sin(2\varphi)}{4}\right)]$$
(20)

 $P_{dt_{red}}$  can be expressed as

$$P_{dt_{red}} = \frac{t_{dt} \cdot f_{SW} \cdot r_{DS} \cdot I_{ac}^2}{8}$$
(21)

Substituting (5), (18), (19), (20), and (21) into (17) yields

$$P_{cond_{M}} = \frac{r_{DS} \cdot \left(\frac{V_{dc} \cdot I_{dc}}{\sqrt{3} \cdot V_{ac,rms} \cdot \cos\varphi}\right)^{2}}{8} + \frac{t_{dt} \cdot f_{SW}}{\pi} \left[V_{f} \cdot \frac{\sqrt{2} \cdot V_{dc} \cdot I_{dc}}{2} (1 - \cos(-\varphi)) + \frac{\left(\frac{\sqrt{2} \cdot V_{dc} \cdot I_{dc}}{\sqrt{3} \cdot V_{ac,rms} \cdot \cos\varphi}\right)^{2}}{4} + \frac{t_{dt} \cdot f_{SW}}{\pi} \left[V_{f} \cdot \frac{\sqrt{2} \cdot V_{dc} \cdot I_{dc}}{\sqrt{3} \cdot V_{ac,rms} \cdot \cos\varphi} + r_{SD} \left(\frac{\varphi}{2} - \frac{\sin(2\varphi)}{4}\right)\right] + \frac{t_{dt} \cdot f_{SW}}{\pi} \left[V_{f} \cdot \frac{\sqrt{2} \cdot V_{dc} \cdot I_{dc}}{\sqrt{3} \cdot V_{ac,rms} \cdot \cos\varphi} + \left(\frac{\sqrt{2} \cdot V_{dc} \cdot I_{dc}}{\sqrt{3} \cdot V_{ac,rms} \cdot \cos\varphi}\right)^{2} + \frac{t_{dt} \cdot f_{SW} \cdot r_{SD} \cdot \left(\frac{\sqrt{2} \cdot V_{dc} \cdot I_{dc}}{\sqrt{3} \cdot V_{ac,rms} \cdot \cos\varphi}\right)^{2}}{8}$$

$$(22)$$

Which simplifies to

$$P_{cond_{M}} = \frac{r_{DS} \cdot V_{dc}^{2} \cdot I_{dc}^{2}}{24 \cdot V_{ac,rms}^{2} \cdot \cos^{2} \varphi} - \frac{\sqrt{6} \cdot f_{SW} \cdot t_{dt} \cdot V_{th} \cdot V_{dc} \cdot I_{dc}}{3\pi \cdot V_{ac,rms}} + \frac{f_{SW} \cdot t_{dt} \cdot r_{SD} \cdot V_{dc}^{2} \cdot I_{dc}^{2}}{12 \cdot V_{ac,rms}^{2} \cdot \cos^{2} \varphi}$$

$$(23)$$

This derivation demonstrates that, for any given operating point of the SiC MOSFET-based inverter,  $P_{cond_M}$  is a function of  $I_{dc}$  and  $V_{dc}$  as all other terms are constant.

Gurpinar and Ozpineci (2018) state that SiC MOSFET forward switching loss can be represented as

$$P_{SW_M} = P_{on} + P_{off} + P_{rr_D} \tag{24}$$

Where  $P_{on}$  is the turn-on switching loss,  $P_{off}$  is the turn-off switching loss, and  $P_{rr_D}$  is the reverse recovery loss across the body diode of the MOSFET. These three terms are assumed to be sufficient as SiC MOSFET datasheets typically incorporate the reverse recovery losses of the device under test into the turn-on loss data. Under the assumption that  $P_{on}$  and  $P_{off}$  change linearly with  $U_{dc}$  and  $i_{ds}$  for the SiC MOSFET C3M0015065K,  $P_{on}$  can be expressed as

$$P_{on} = \frac{f_{SW} \cdot I_{ac} \cdot V_{dc} \cdot E_{on,test}}{2\pi \cdot V_{DS,test} \cdot I_{DS,test}}$$
(25)

Where  $E_{on,test}$  is turn-on switching loss energy,  $I_{DS,test}$  is drain-source current,  $V_{DS,test}$  is drain-source voltage, all of which are normalized to the inverter operating condition. Similarly,  $P_{off}$  can be expressed as

$$P_{off} = \frac{f_{SW} \cdot I_{ac} \cdot V_{dc} \cdot E_{off,test}}{2\pi \cdot V_{DS,test} \cdot I_{DS,test}}$$
(26)

Where  $E_{on,test}$  is turn-off switching loss energy.  $P_{rr_D}$  can be expressed as

$$P_{rr_D} = \frac{f_{SW} \cdot t_b \cdot I_{RRM} \cdot V_{dc}}{12} \tag{27}$$

Where  $I_{RRM}$  is the peak reverse recovery of the SiC MOSFET diode and  $t_b$  is the time for  $I_{RRM}$  to decay to zero []. Substituting (5), (25), (26), and (27) into (24) yields

$$P_{SW_M} = \frac{f_{SW} \cdot \frac{\sqrt{2} \cdot V_{dc} \cdot I_{dc}}{\sqrt{3} \cdot V_{ac,rms} \cdot \cos \varphi} \cdot V_{dc} \cdot E_{on,test}}{2\pi \cdot V_{DS,test} \cdot I_{DS,test}} + \frac{f_{SW} \cdot \frac{\sqrt{2} \cdot V_{dc} \cdot I_{dc}}{\sqrt{3} \cdot V_{ac,rms} \cdot \cos \varphi} \cdot V_{dc} \cdot E_{off,test}}{2\pi \cdot V_{DS,test} \cdot I_{DS,test}} + \frac{f_{SW} \cdot \frac{\sqrt{2} \cdot V_{dc} \cdot I_{dc}}{\sqrt{3} \cdot V_{ac,rms} \cdot \cos \varphi}}{2\pi \cdot V_{DS,test} \cdot I_{DS,test}}$$
(28)

Which simplifies to

$$P_{SW_M} = \frac{\sqrt{6} \cdot f_{SW} \cdot E_{on,test} \cdot V_{dc}^2 \cdot I_{dc}}{6\pi \cdot V_{ac,rms} \cdot V_{DS,test} \cdot I_{DS,test} \cdot \cos\varphi} + \frac{\sqrt{6} \cdot f_{SW} \cdot E_{off,test} \cdot V_{dc}^2 \cdot I_{dc}}{6\pi \cdot V_{ac,rms} \cdot V_{DS,test} \cdot I_{DS,test} \cdot \cos\varphi} + \frac{f_{SW} \cdot t_b \cdot I_{RRM} \cdot V_{dc}}{12}$$

$$(29)$$

This derivation demonstrates that, for any given operating point of the SiC MOSFET-based inverter,  $P_{SW_M}$  is a function of  $I_{dc}$  and  $V_{dc}$  as all other terms are constant.

The total SiC MOSFET power loss is

$$P_M = P_{cond_M} + P_{SW_M} \tag{30}$$

Substituting (23) and (29) into (30) yields  

$$P_{M} = \frac{r_{DS} \cdot V_{dc}^{2} \cdot I_{dc}^{2}}{24 \cdot V_{ac,rms}^{2} \cdot \cos^{2} \varphi} - \frac{\sqrt{6} \cdot f_{SW} \cdot t_{dt} \cdot V_{th} \cdot V_{dc} \cdot I_{dc}}{3\pi \cdot V_{ac,rms}} + \frac{f_{SW} \cdot t_{dt} \cdot r_{SD} \cdot V_{dc}^{2} \cdot I_{dc}^{2}}{12 \cdot V_{ac,rms}^{2} \cdot \cos^{2} \varphi} - \frac{\frac{f_{SW} \cdot t_{dt} \cdot r_{DS} \cdot V_{dc}^{2} \cdot I_{dc}}{3\pi \cdot V_{ac,rms}} + \frac{\sqrt{6} \cdot f_{SW} \cdot E_{on,test} \cdot V_{dc}^{2} \cdot I_{dc}}{12 \cdot V_{ac,rms}^{2} \cdot \cos^{2} \varphi} + \frac{\sqrt{6} \cdot f_{SW} \cdot E_{on,test} \cdot V_{dc}^{2} \cdot I_{dc}}{6\pi \cdot V_{ac,rms} \cdot V_{DS,test} \cdot I_{DS,test} \cdot \cos \varphi} + \frac{\sqrt{6} \cdot f_{SW} \cdot E_{off,test} \cdot V_{dc}^{2} \cdot I_{dc}}{12}$$

$$(31)$$

This derivation demonstrates that, for any given operating point of the SiC MOSFET-based inverter,  $P_M$  is a function of  $I_{dc}$  and  $V_{dc}$  as all other terms are constant.

#### 2. Modeling Algorithm

The derivations in the previous section demonstrate that the traction inverter power loss can be estimated from DC bus voltage and current. Therefore, in a vehicle simulation model, power loss and efficiency of the traction inverter can be extracted from lookup tables instead of conducting a power electronics simulation at every single switching cycle. In this research, traction inverter efficiency maps were developed in PSpice with manufacturer semi-conductor models directly applied. To estimate power loss and efficiency of 2 switch candidates, Si IGBT IKW50N60DTP and SiC MOSFET C3M0015065K were utilized to develop 3-phase inverter models in PSpice with RL loads. For the SiC-based inverter, there are 4 MOSFETs in parallel on each arm; while for the IGBT-based counterpart, there are 3 switches in parallel. The switching frequencies were set to 50kHz for the SiC MOSFET-based inverter and 10kHz for the Si IGBT-based inverter, repectively. By changing the DC bus voltage and modulation index, efficiency lookup tables of the SiC MOSFET- and Si IGBT-based inverters vs. DC bus voltage and modulation index, as shown in Figure 1 (a) and (b) respectively. The inverter efficiency maps were then embedded into the vehicle simulation model.



Figure 1. Traction Inverter Efficiency vs. DC Bus Voltage and Current



Figure 2. Backward Vehicle Simulation Architecture

The vehicle model was developed with backward architecture as shown in Figure 2. The vehicle dynamics block calculates the mechanical power that the e-motor needs to provide to overcome road load from the speed profile input. The e-motor block converts the mechanical power request to electric power (AC) request. The inverter block with embedded efficiency maps obtained from PSpice converts the power request from AC power to DC power, which charges/discharges the battery. Finally, the battery block estimates DC bus voltage and current to determine real-time inverter efficiency.

In the vehicle dynamics block, the mechanical power request is calculated as

$$P_{mech} = (k \cdot m \cdot a) + (F_{RL} \cdot v) \tag{32}$$

Where k is the mass factor to equivalent rotating parts inertia, m is the total weight of vehicle curb, driver and payload, a is the vehicle acceleration;  $F_{RL}$  is the road load force, and v is the vehicle speed.  $F_{RL}$  is calculated as

$$F_{RL} = F_{RR} + F_{AD} + F_{HC} \tag{33}$$

Where  $F_{RR}$  is the tire rolling resistance,  $F_{AD}$  is the air drag force, and  $F_{HC}$  is the hill climbing resistance.  $F_{RR}$  can be expressed as

$$F_{RR} = m \cdot g \cdot F_R \cdot \cos\theta \tag{34}$$

Where g is the acceleration due to gravity (9.8 N/kg),  $F_R$  is the tire rolling friction coefficient, and  $\theta$  is the road grade in degrees.  $F_{AD}$  from (33) can be expressed as

$$F_{AD} = 0.5 \cdot \rho_{air} \cdot A \cdot C_d \cdot v^2 \tag{35}$$

Where  $\rho_{air}$  is the air density, A is the vehicle frontal cross sectional area, and  $C_d$  is the air drag coefficient.  $F_{HC}$  is calculated as

$$F_{HC} = m \cdot g \cdot \sin \theta \tag{36}$$

The vehicle modeled in this research was a Tesla Model S with a single motor. The vehicle parameters are shown in Table 1 (Palin et al. 2012).

Description	Value
Vehicle Curb Weight	2107kg
Driver and Load Weight	100kg
Vehicle Cross Section	3.4m <sup>2</sup>
Tesla Drag Coefficient	0.208
Rolling Friction Coefficient	0.04
Mass Factor	1.1
Differential Gear Ratio	9.73
Tire Radius	0.352m
Driveline Efficiency	98%

#### Table 1. Tesla Model S Single Motor Vehicle Parameters

The e-motor block is modeled as an efficiency map from test data, shown in Figure 3 (Thomas et al. 2020). In this plot, positive torque indicates generated torque output and negative torque indicates regenerative braking torque.



Figure 3. Motor Efficiency Map

The inverter block with embedded efficiency maps from PSpice converts AC power to DC power that charges/discharges the battery. The DC power is presented to the inverter block as

$$P_{dc} = \begin{cases} P_{mech} \div \eta_{mtr} \div \eta_{inv} \text{ if } P_{mech} > 0\\ P_{mech} \cdot \eta_{mtr} \cdot \eta_{inv} \text{ if } P_{mech} < 0 \end{cases}$$
(37)

Where  $\eta_{mtr}$  and  $\eta_{inv}$  are motor and inverter efficiency, respectively. The battery block is formed by a state-ofcharge (SOC) calculation module and a 2RC equivalent circuit model (Rajanma et al. 2020), as shown in Figure 4.



Figure 4. Battery Model Architecture

The SOC is estimated via the coulomb counting method, expressed as

$$SOC = SOC_{initial} - \frac{\int i_{dc}(t)dt}{C_{rate}}$$
(38)

Where  $SOC_{initial}$  is the initial SOC, and  $C_{rate}$  is the rated battery capacity in Ah. The 2RC equivalent battery model is shown in Figure 5, in which the terminal voltage  $V_t$  is determined as

$$V_t = OCV - i_{dc}R_0 - \frac{1}{C_1} \int (i_{dc} - \frac{V_1}{R_1}) dt - \frac{1}{C_2} \int (i_{dc} - \frac{V_2}{R_2}) dt$$
(39)

Where OCV is the battery open circuit voltage, which is determined by the SOC.  $i_{dc}$  is he battery current calculated from DC power request and terminal voltage.  $V_1$  and  $V_2$  are the voltages of the first and second RC branch, respectively.



Figure 5. Battery Model Architecture

#### **3. Simulation Results**

Using the developed vehicle model, which includes an embedded inverter efficiency map, simulations have been performed for both Si IGBT- and SiC MOSFET-based traction inverters. A speed input profile that combines the Urban Dynamometer Driving Schedule (UDDS) and the Highway Fuel Economy Test (HFET) drive cycles was used, which is depicted in Figure 6. This combination allows for estimations under both urban and highway driving conditions. Figure 7 illustrates the simulated efficiency of the Si IGBT- and SiC MOSFET-based inverters, and Figure 8 highlights the power loss associated with each.



Figure 6. UDDS + HFET Drive Cycle



Figure 7. Inverter Efficiency of UDDS+HFET Cycle



Figure 8. Inverter Power Loss of UDDS+HFET Cycle

Upon examining Figures 7 and 8, it is evident that the SiC MOSFET-based inverter exhibits higher and more stable efficiency than the Si IGBT-based inverter, translating to a significant reduction in power loss during the combined UDDS+HFET drive cycle. By integrating the power loss over this cycle, it was found that the total energy losses for SiC MOSFET- and Si IGBT-based inverters amount to 68.38Wh and 925.9Wh, respectively. This stark difference underscores the superior efficiency and lower energy loss characteristics of the SiC MOSFET-based inverter compared to its Si IGBT counterpart.

#### 4. Conclusion

This research introduces a novel method for simulating electric vehicle inverter efficiency and estimating power loss. The method employs switch-cycle based simulation in PSpice to generate efficiency lookup tables corresponding to DC bus voltage and current of inverters with different semiconductors. A vehicle model with an embedded inverter efficiency map can be used to carry out simulations with durations in the thousands of seconds. The developed model, based on a Tesla Model S, has been tested with two candidate traction inverters, Si IGBT IKW50N60DTP and SiC MOSFET C3M0015065K, respectively. Simulation results confirm that SiC MOSFET proves to be a superior candidate compared to Si IGBT for traction inverter development. By adopting SiC MOSFET as the power switch, inverter efficiency can be maintained in the >99% range, saving 92.6% in energy loss.

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