

Bilevel Robust Optimization for Design and Pricing of Electric Vehicle Battery Reuse Network

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Abstract

The rapid proliferation of electric vehicles has led to a significant increase in the quantity of used electric vehicle batteries (EVBs). This necessitates the design of a waste reverse supply chain to reuse and recycle EVBs and protect the environment. This study examines an integrated reuse network design and pricing problem for EVBs. To design a reliable EVB reuse network to hedge against return quantity uncertainty, we present two bilevel globalized distributionally robust (GDR) design and pricing models. We derive computationally tractable reformulations of GDR expectation and chance constraints. For the resulting joint chance-constrained model, we propose a tailored branch-and-cut (B&C) algorithm and introduce a strengthened formulation to speed up the solution process. A real-world case study is conducted to validate the superiority of the proposed methods and examine the impacts of key model parameters on profitability. Results demonstrate that the globalized distributionally robust optimization models exhibit greater robustness than stochastic optimization models. The computational performance of the tailored B&C algorithm incorporating a strengthened formulation is assessed compared to the standard solver. Finally, based on the numerical results, we derive managerial insights from the analytical findings.

Keywords

Network design; pricing; used electric vehicle battery; distributionally robust optimization; algorithm

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Guoqing Zhang, PEng, is a Professor of Industrial Engineering in the Supply Chain and Logistics Optimization Research Lab at the Department of Mechanical, Automotive & Materials Engineering, University of Windsor. His research interests include supply chain management and optimization, operations research, manufacturing modeling, e-commerce, warehouse management, data-driven optimization, machine learning, and intelligent decision support systems. He has published over 100 articles in these areas. Dr. Zhang's research is supported by NSERC, MITACS, and CFI. He has provided consulting services to several world-leading companies in the automotive, energy, airline, and food industries. In 2015, his team received the CORS Practice Prize. Additionally, he developed a solver for large-scale linear programming based on the interior point method.